

重・超重核領域における原子核の崩壊様式の理論及びr過程 元素合成への応用

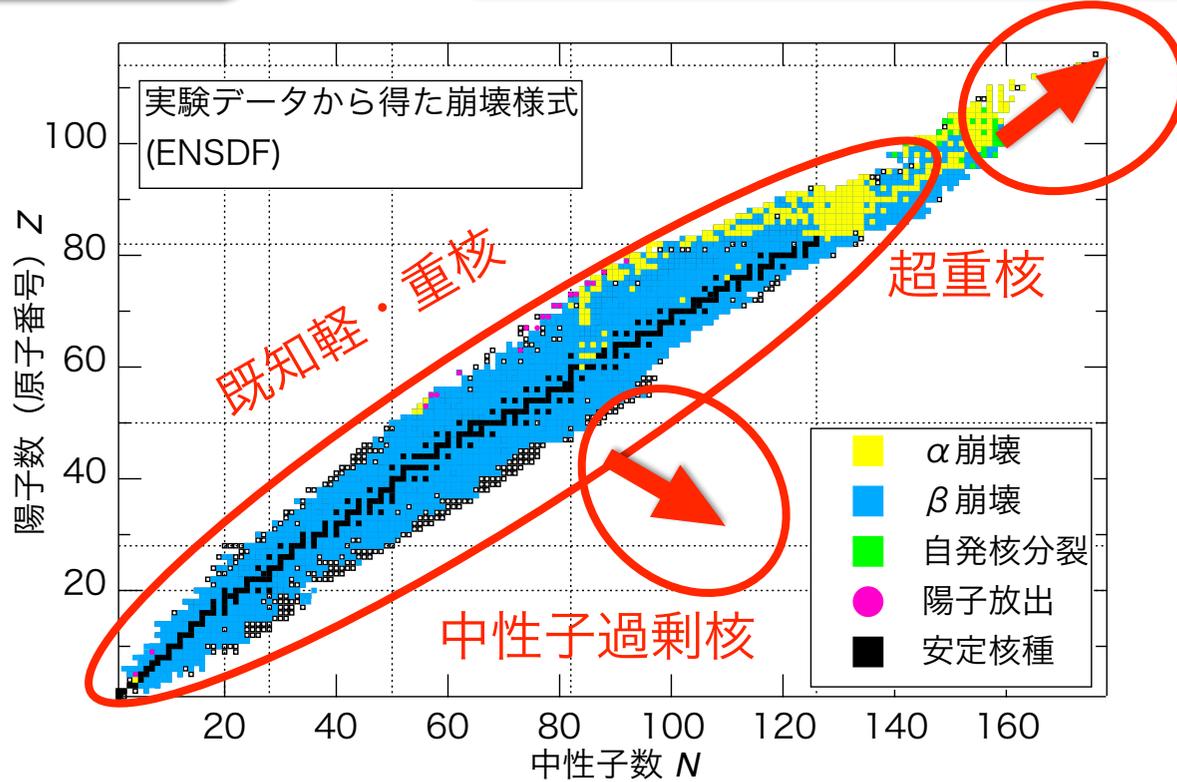
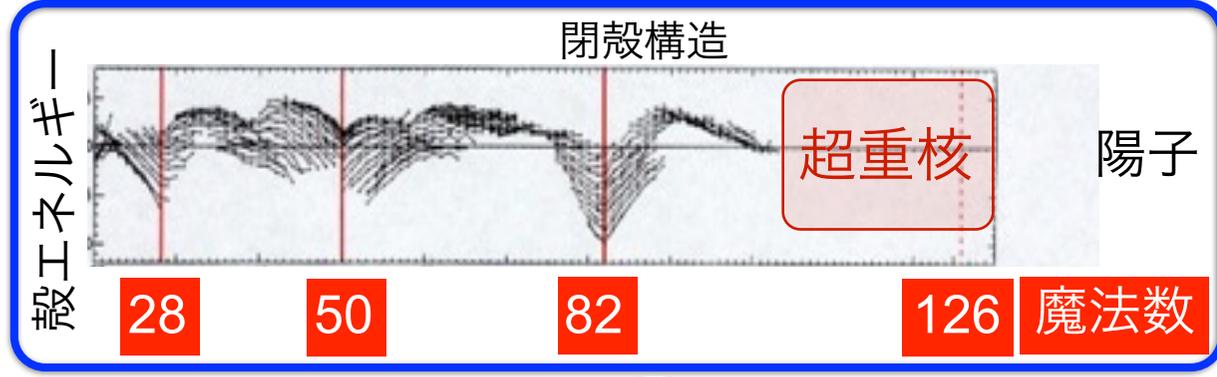
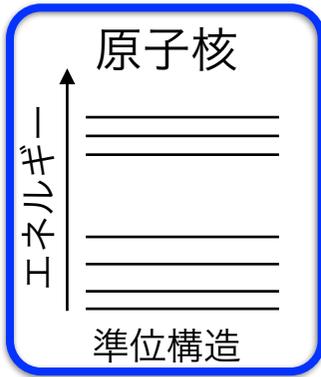
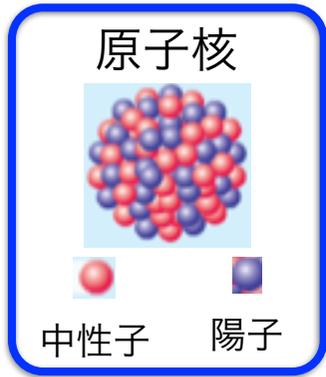
小浦寛之

日本原子力研究開発機構

先端基礎研究センター

1. 原子核（同位体）探索の現状
2. 原子核質量模型及び原子核崩壊計算
3. 核分裂
4. r過程における核分裂の影響

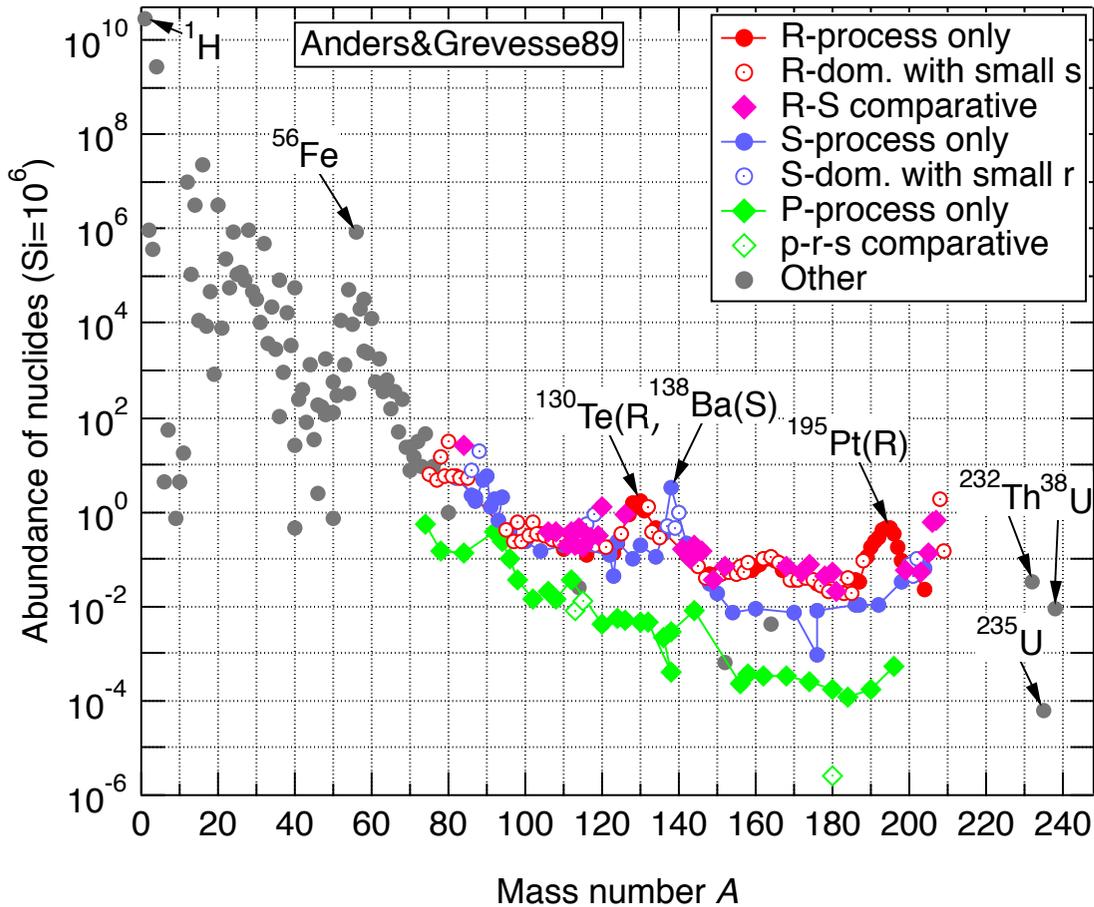
目的：原子核構造・崩壊の（核図表上の）大域的理解



原子核の崩壊様式(小浦, 橘, 日本物理学会誌 60,717-724 (2005))

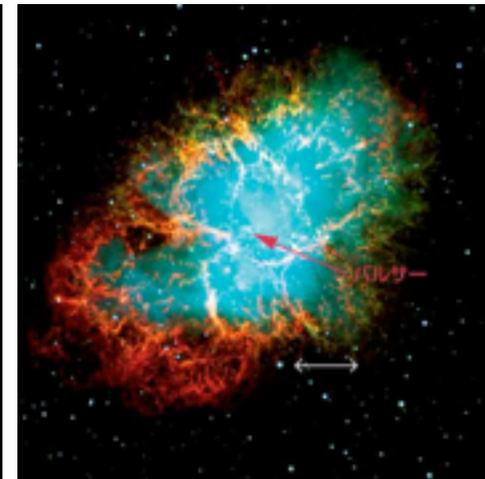
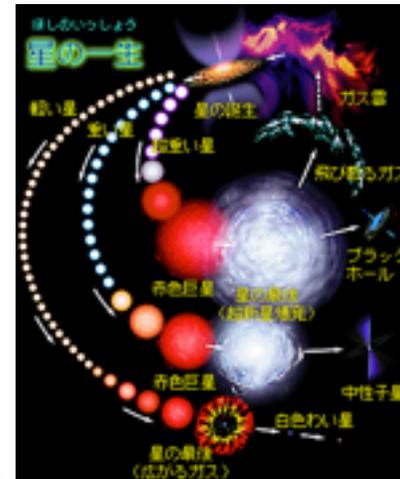
重・超重原子核の核構造、原子核崩壊を理論的に研究

目的：原子核の起源の理論的探求 —星の元素合成—



小浦、核データニュース101, (2012)

- **S-process:**遅中性子捕獲過程。赤色巨星などで数千年程度かけて中性子捕獲反応が進む。
- **R-process:**速中性子捕獲過程。超新星爆発などで数秒で中性子捕獲反応が進む。



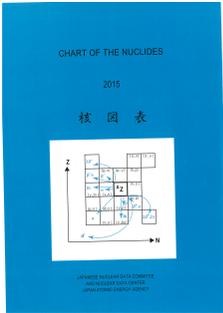
太陽系における同位体の存在比（観測値）

鉄(Fe)より重い原子核の現在の理解

- **Fe-Bi**：赤色巨星によって作られた(s過程(slow process))
- **Fe-U**：超新星爆発によって作られた(r過程(rapid process))

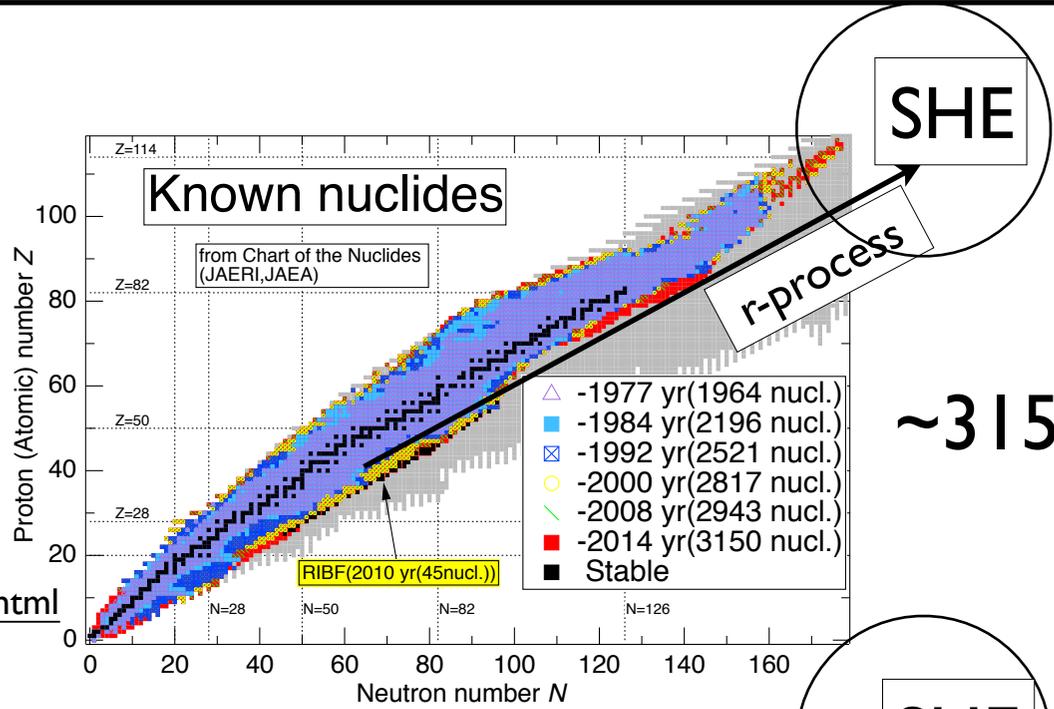
Search of nuclei: current understandings

Identified



taken from Chart of the nuclides by JAERI and JAEA (HK, et al., 2015)

wwwndc.jaea.go.jp/CNI4/index.html



We know now

~3150 nuclei

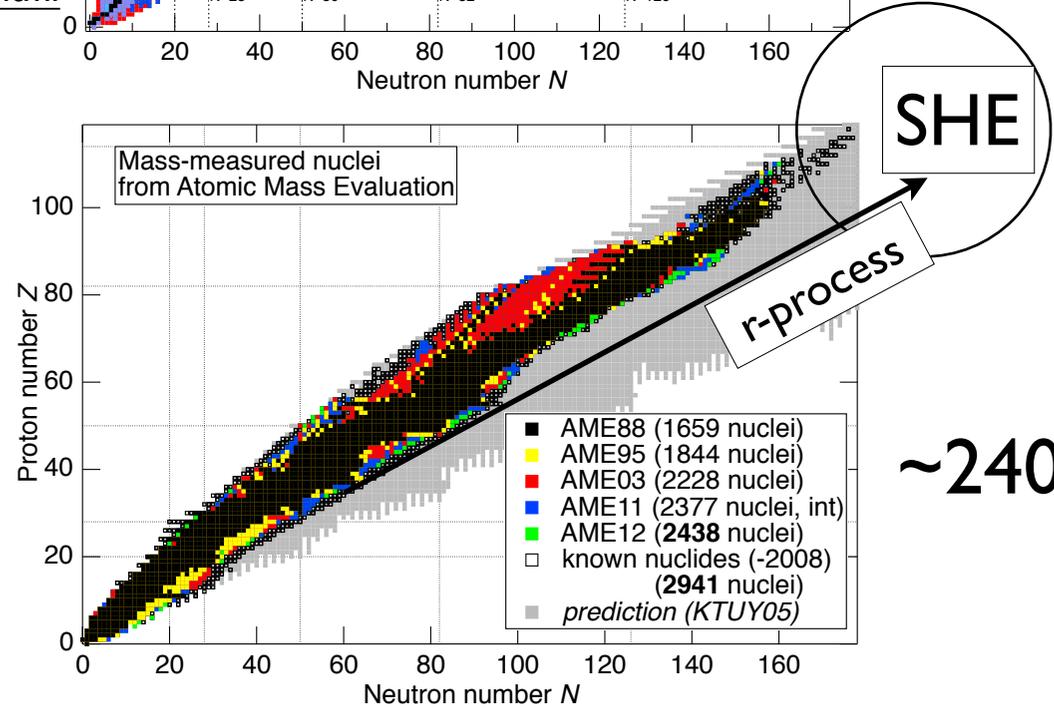
and

Mass-measured



AME2012 is updated three years ago

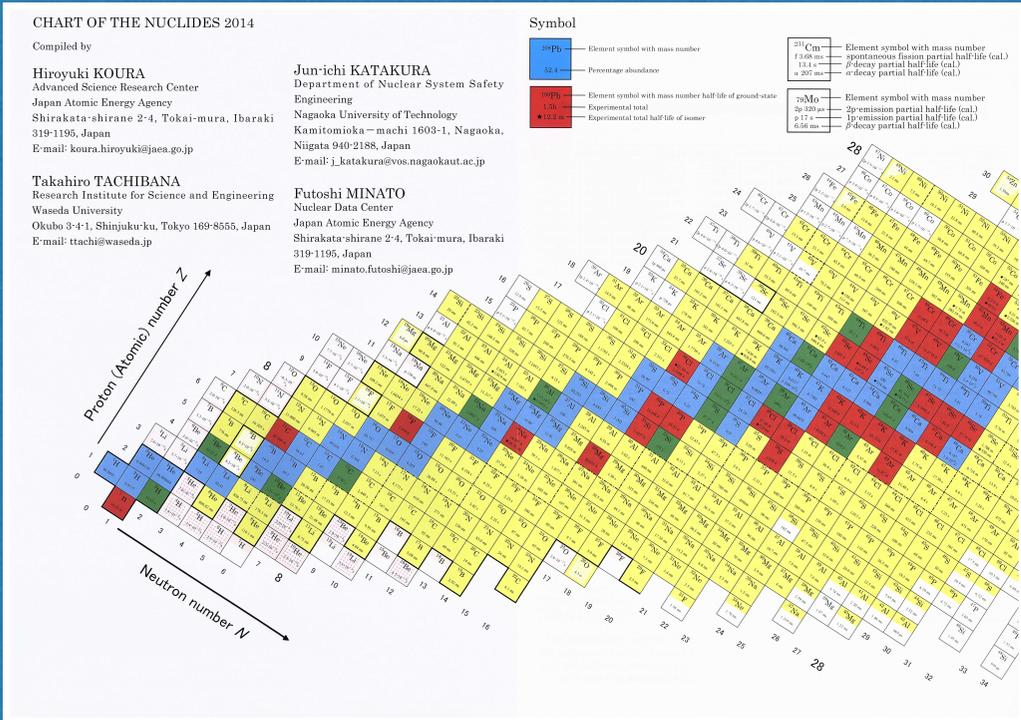
amdc.in2p3.fr/mastables/file.html



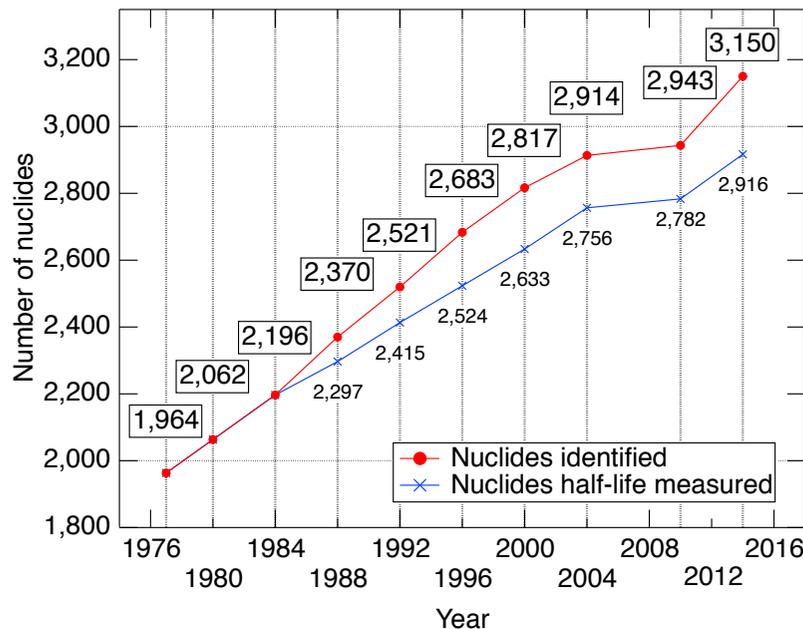
We know now masses of

~2400 nuclei

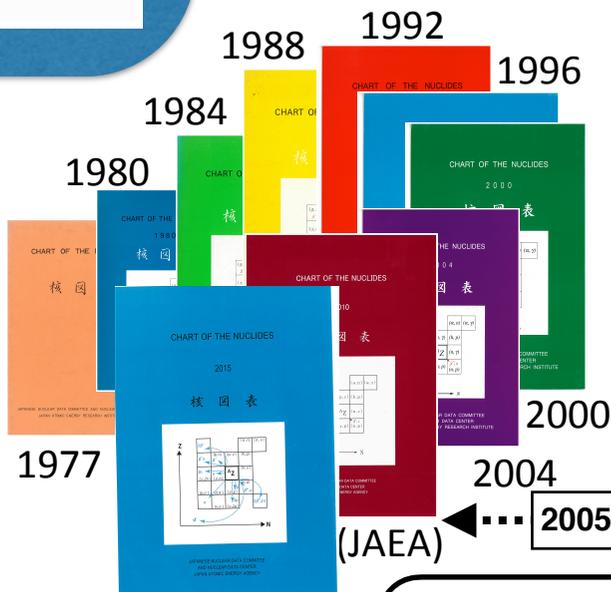
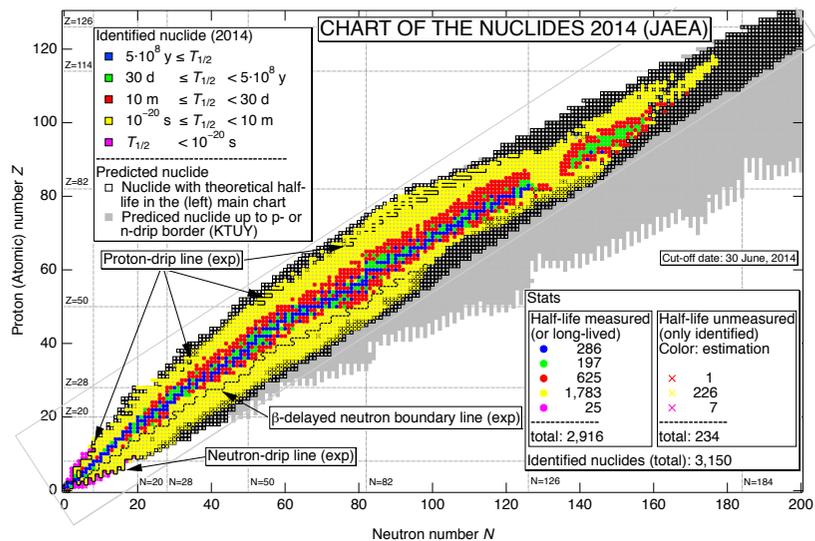
A tool to understand overview of nuclear decay



A4-size, folded in 16 pages



Identified isotopes



- Compilers:
- Y. Yoshizawa (1977 - 1988)
 - T. Horiguchi (1977 - 2004)
 - M. Yamada (1977 - 1988)
 - T. Tamura (1992)
 - J. Katakura (1992 -)**
 - T. Tachibana (1992 -)**
 - H. Koura (2000 -)**
 - F. Minato (2014 -)**

Person: current compiler

2005: JAERI to JAEA

Press release

<http://www.jaea.go.jp/02/press2014/p1503120/>

CHART OF THE NUCLIDES 2014

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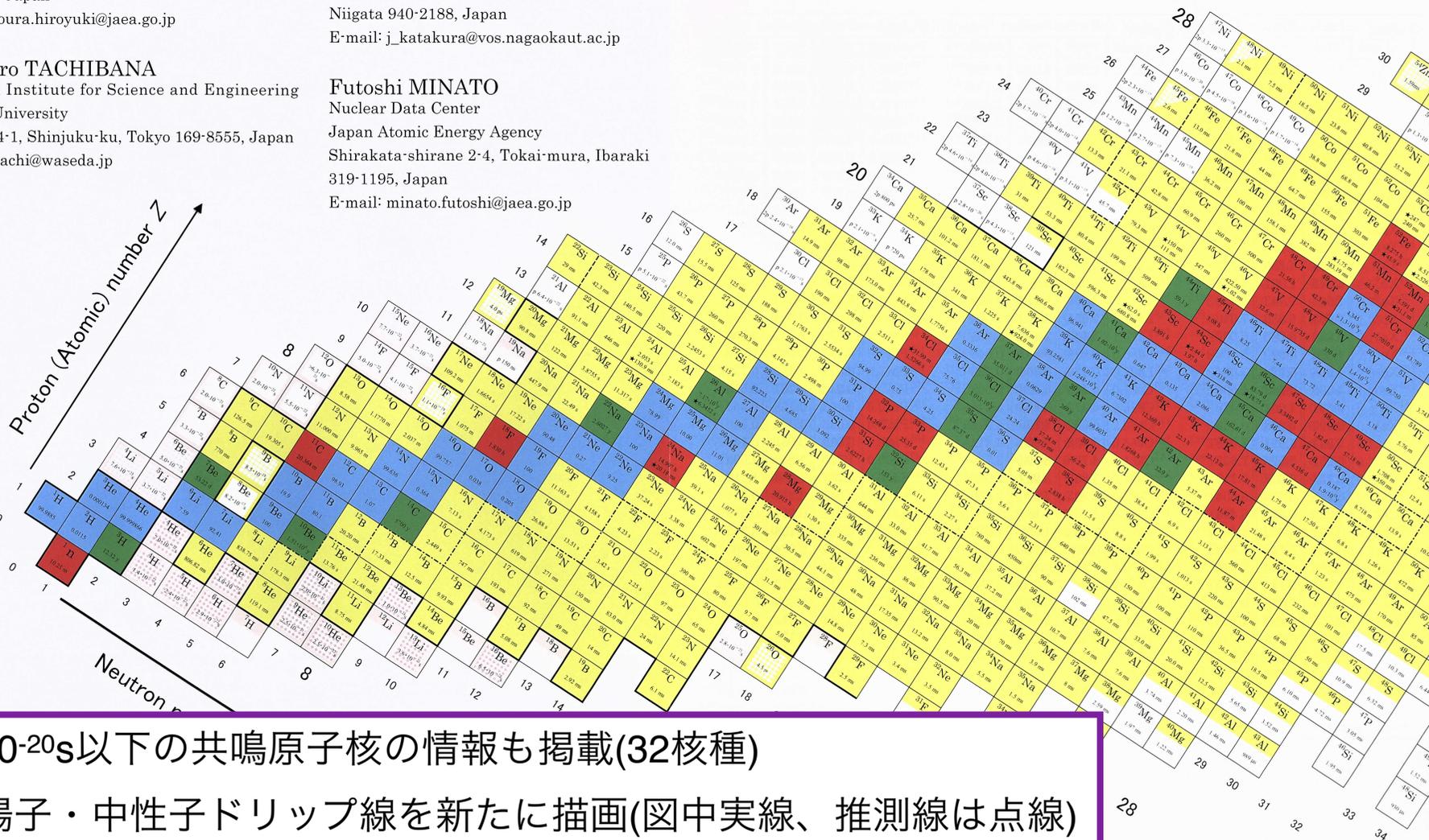
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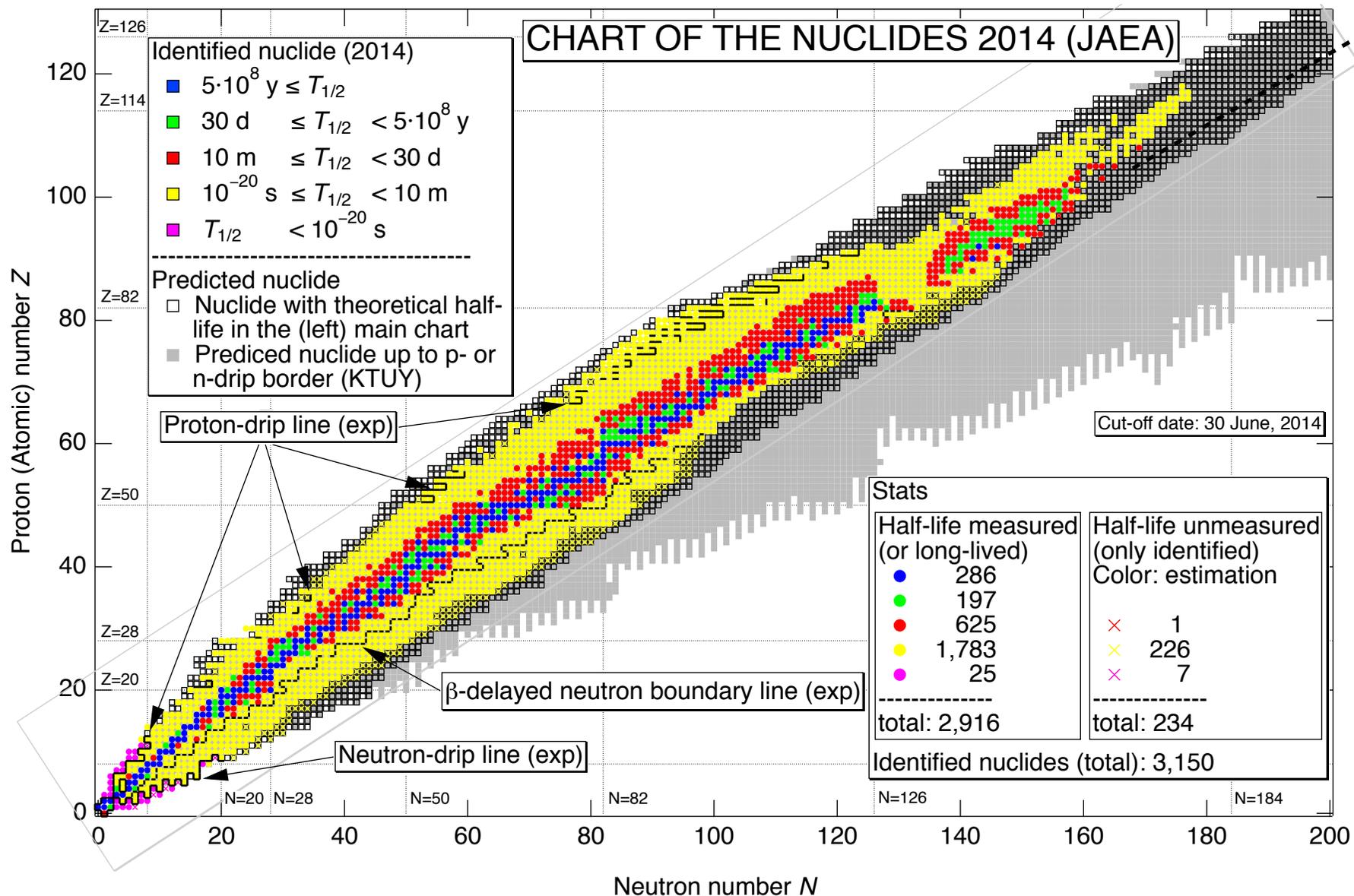
Symbol

	Element symbol with mass number Percentage abundance
	Element symbol with mass number half-life of ground-state Experimental total Experimental total half-life of isomer
	Element symbol with mass number spontaneous fission partial half-life (cal.) β -decay partial half-life (cal.) α -decay partial half-life (cal.)
	Element symbol with mass number 2p 320 μ s 1p 17 s β -decay partial half-life (cal.)



- 10^{-20} s以下の共鳴原子核の情報も掲載(32核種)
- 陽子・中性子ドリップ線を新たに描画(図中実線、推測線は点線)
- β 崩壊遅発中性子放出核の境界線を掲載(図中破線)

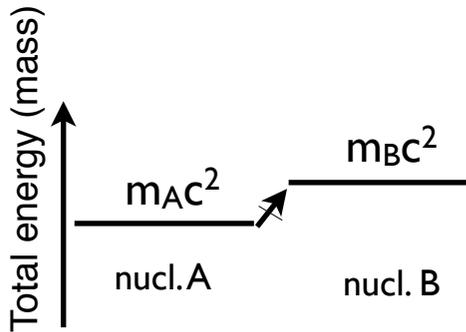
Overview of identified nuclei from Chart of the Nuclides 2014



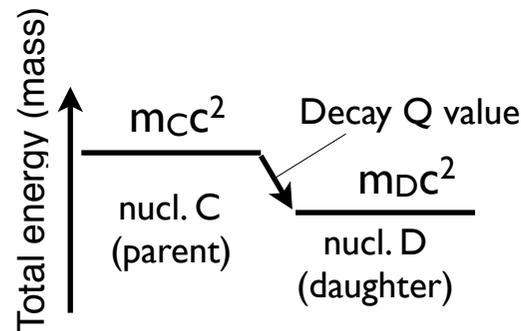
Why nuclear mass?

- Equivalence to **total energy** of nucleus: $E = mc^2$
 - Governing nuclear reaction and decay modes

$$E = mc^2$$

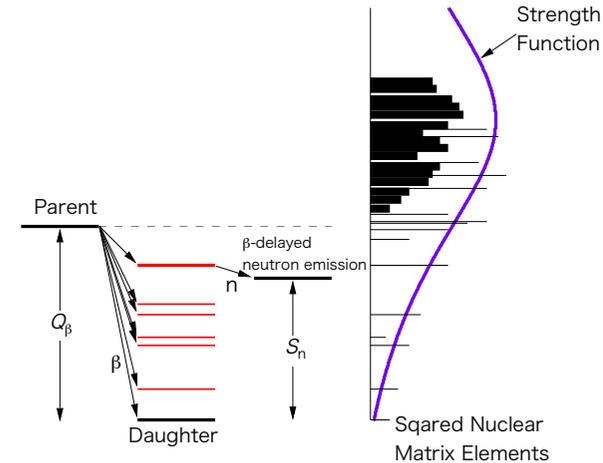


Nucleus A can not decay.



Nucleus C can decay.

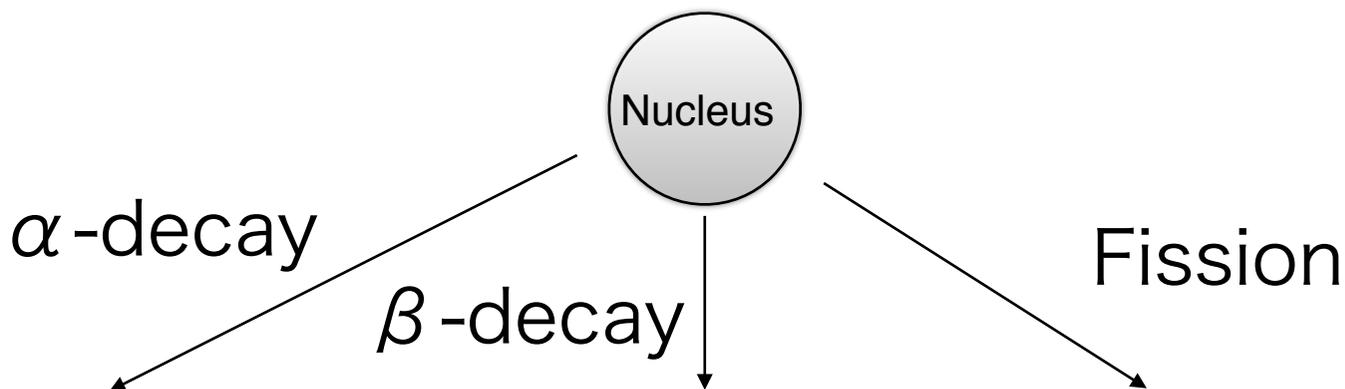
Diff. of mass(total energy) determine the direction of nuclear decay.



$$\lambda = \frac{1}{2\pi^3} \int_{-Q}^0 \sum_{\Omega} |g_{\Omega}|^2 \cdot |M_{\Omega}(E_g)|^2 f(-E_g + 1) dE_g$$

Decay rate of beta-decay

Prediction of nuclear decays



α -decay : tunneling

残留核 Penetrability $V(x)$ α 粒子 E → emit

r_{in} r_{out}

Nuclear force +Coulomb

Req.: Mass diff. (Q-value)

β -decay : weak int.

Parent St. func. |Nuc. Mat. Ele.²

Daughter

Req.: Mass diff. (Q-value)

Fission : Potential ag. shape

²⁸⁹Ds₁₁₀

サドル点 核分裂

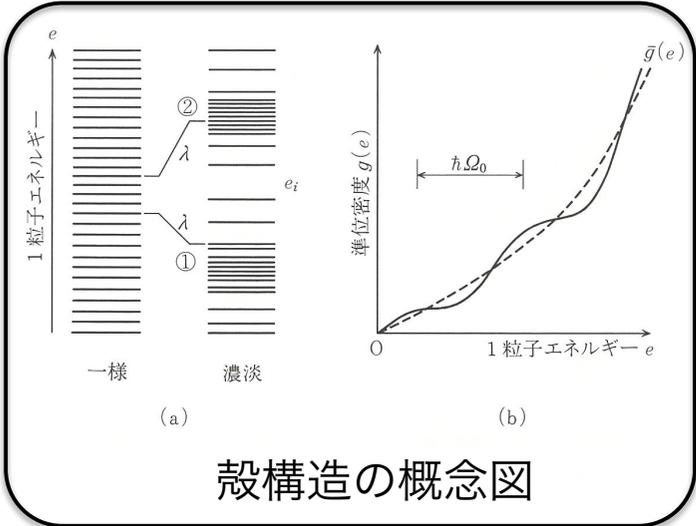
基底状態 サドル点

Req.: Description of shape



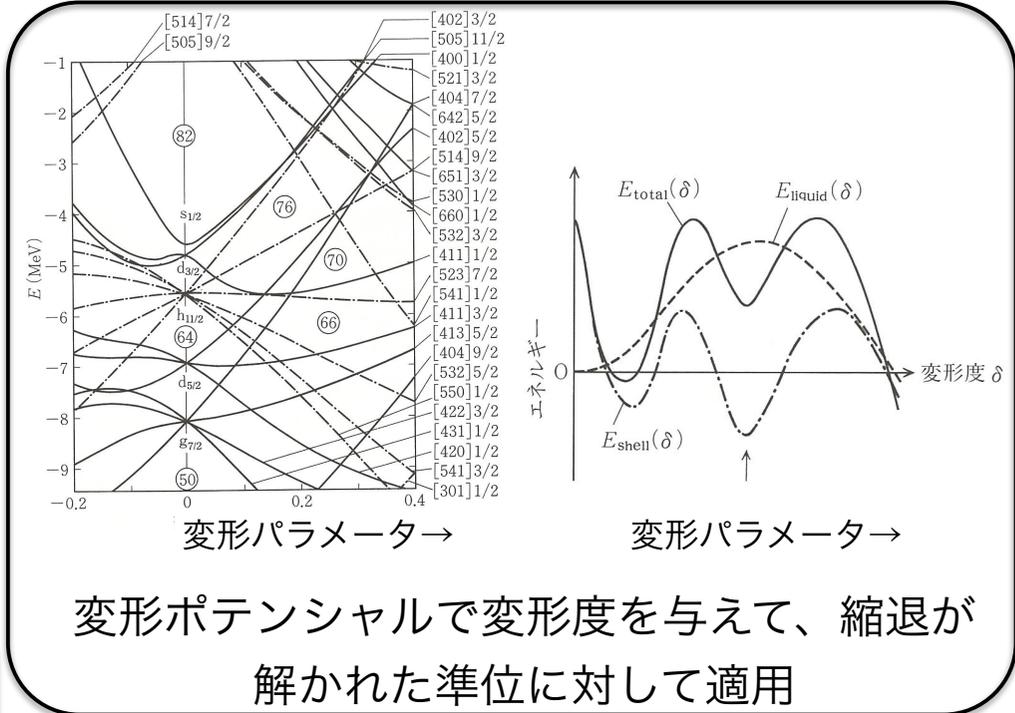
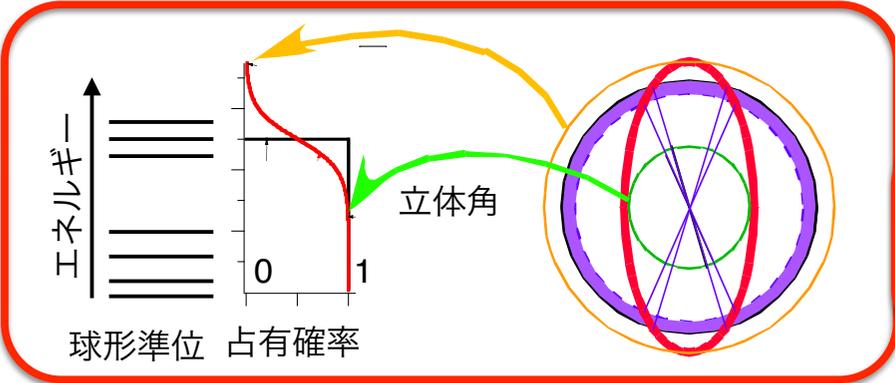
Nuclear masses (and description of nuclear shape) are required.

Mass model: Spherical-basis method (KTUY)



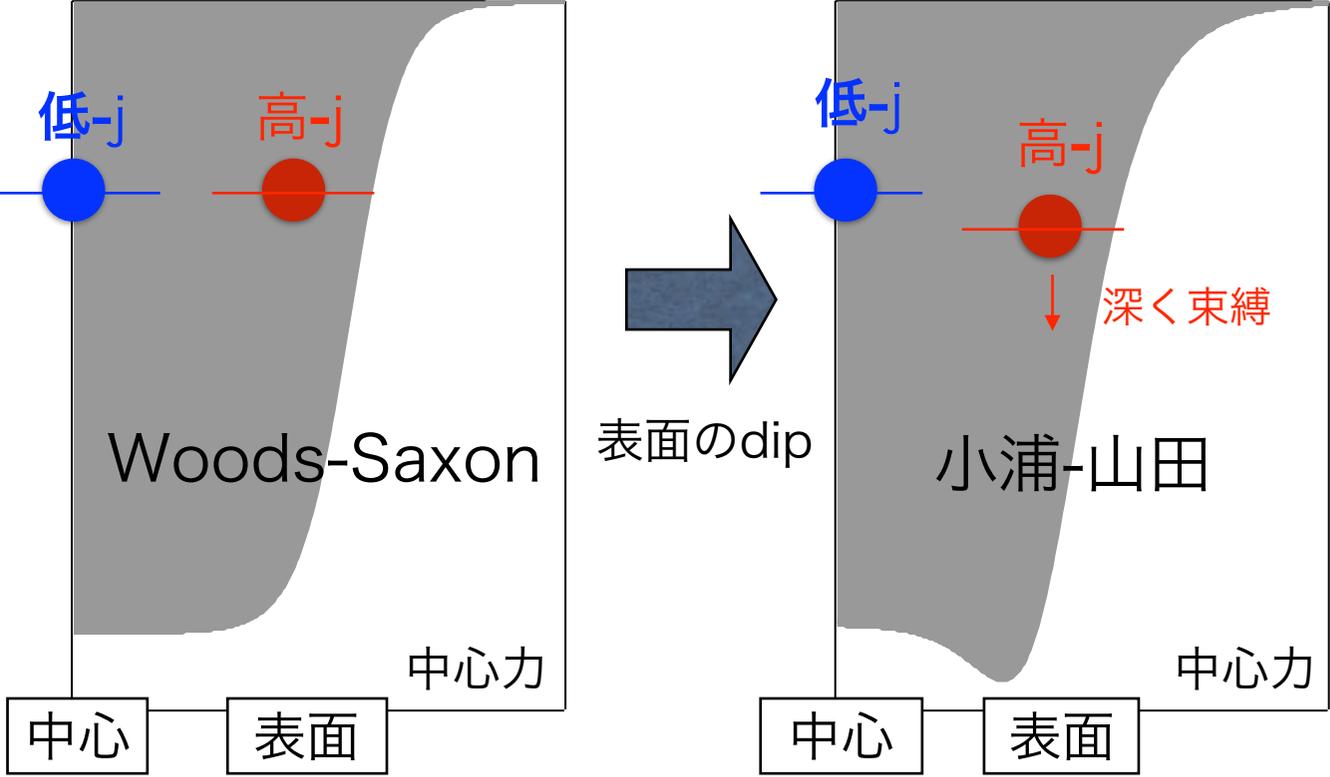
Nilsson-Strutinsky 法
変形単一粒子ポテンシャルより準位を得、それに粒子を積み上げることにより求める

球形基底の方法(今回用いた方法)
球形単一粒子ポテンシャルより準位を得、変形状態を球形状態の配位混合として扱う

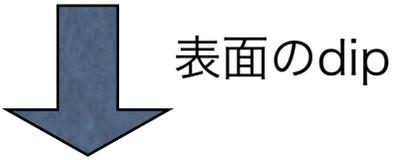


実際の計算：球形殻Eの重み付き和
球形殻E：球形準位の積分
重み：立体角(占有確率)の微分

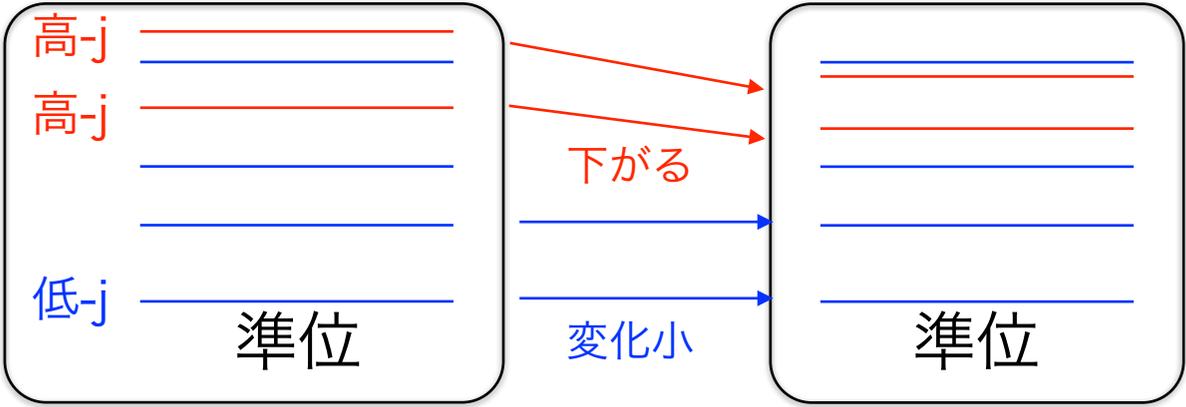
高スピン軌道(j)の核子に対する役割



低-j:原子核の**中心**に分布
高-j:原子核の**表面**に分布



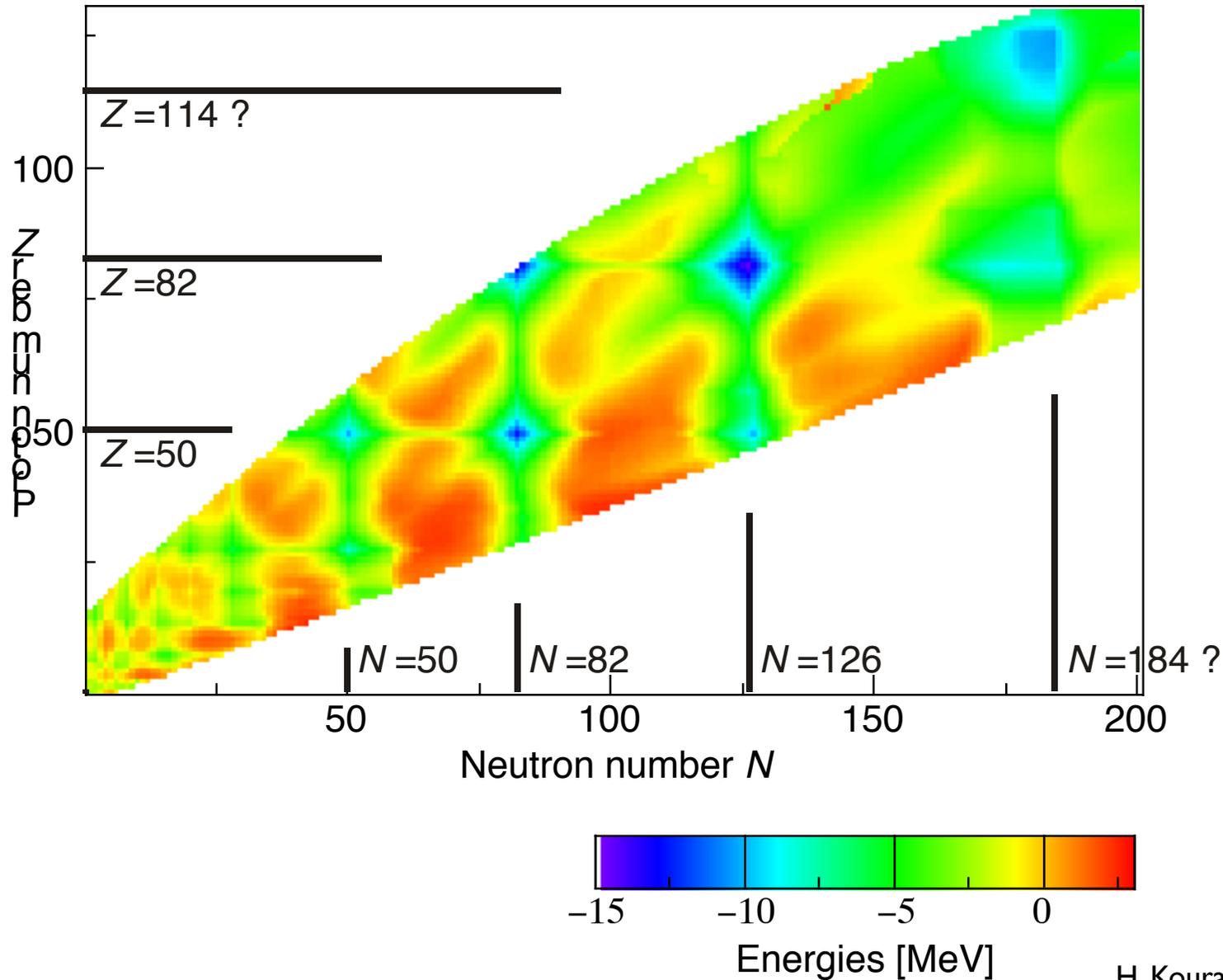
高-j核子:**より深い準位へ**
→実験準位をW-Sよりよく再現することに成功



^{132}Sn , ^{208}Pb 等の2重球形閉殻

Nuclear shell energy

Nuclear shell energies $E_{sh}(Z, N)$

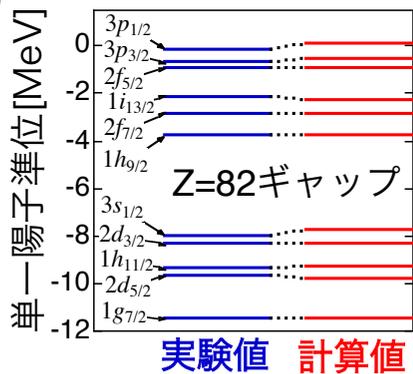
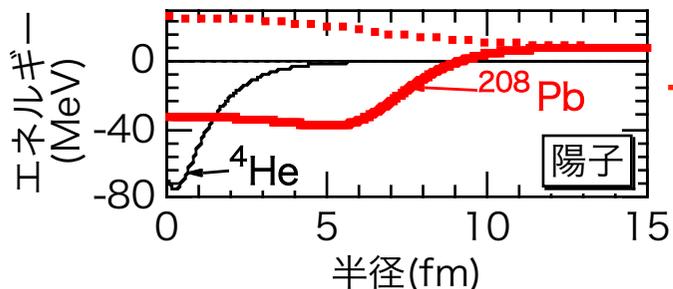


KTUY質量公式

(まとめ)

(1) 球形単一粒子ポテンシャル

- 5パラメータ, Z, Nの関数



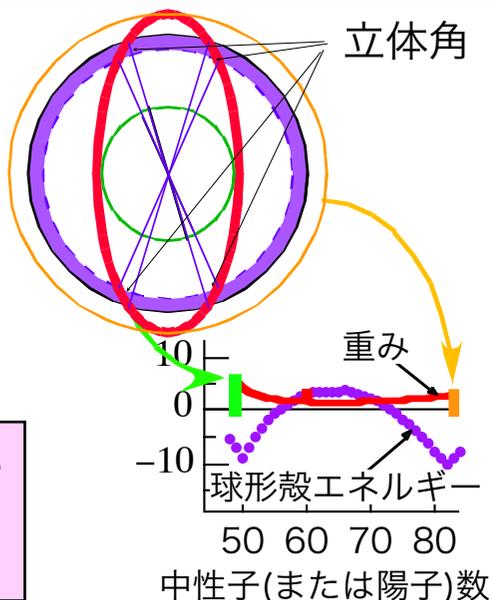
単一陽子準位 (208Pb)

4Heから208Pbにわたり精度の高い単一粒子準位の再現を実現

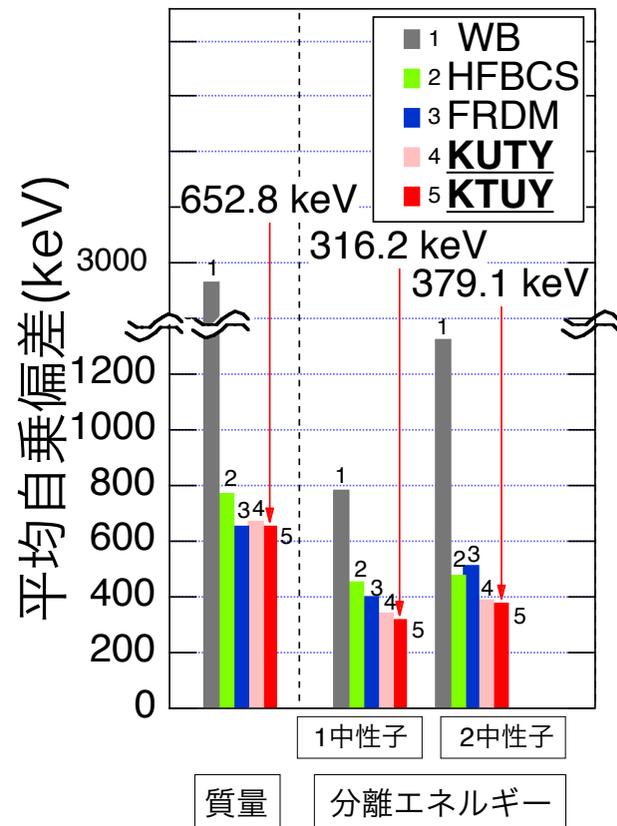
(2) 変形殻エネルギー計算

- (1)の球形ポテンシャルを使用
- 変形原子核の殻エネルギーを球形殻エネルギーの重み付き和として与える
- 重み:分割球形核が占める立体角の微係数

原子核質量の殻エネルギーの新たな計算方法



(3) 質量再現性



実験値との平均自乗偏差 (2149核種)

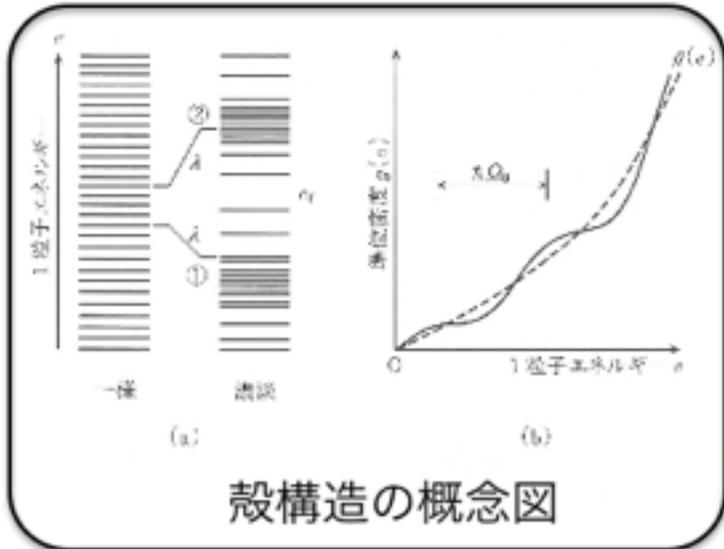
他モデルと比べて高い質量値再現性を実現



Fission

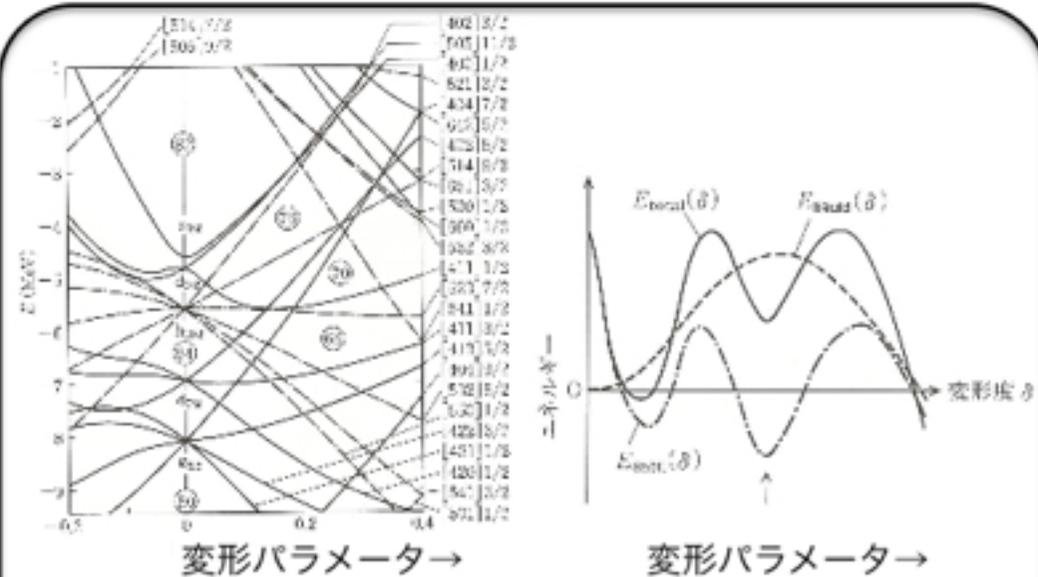


核分裂障壁の理論計算



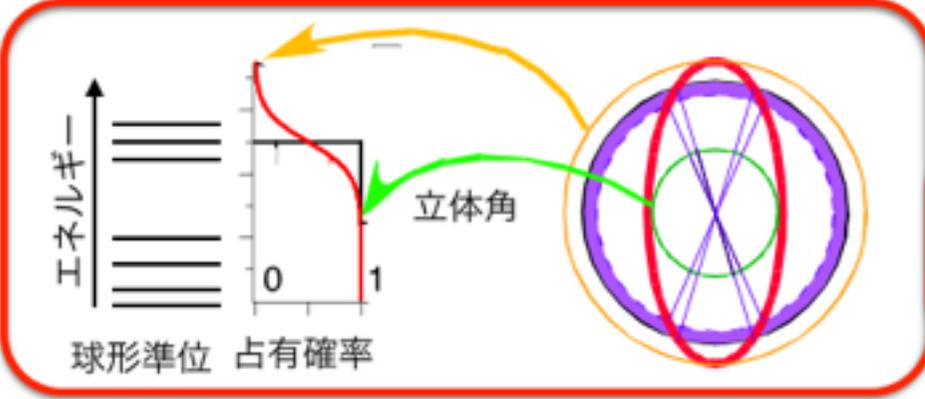
Nilsson-Strutinsky 法

変形単一粒子ポテンシャルより準位を得、
それに粒子を積み上げることにより求める



変形ポテンシャルで変形度を与えて、縮退が
解かれた準位に対して適用

球形基底の方法(今回用いた方法)
球形単一粒子ポテンシャルより準位を得、
変形状態を球形状態の配位混合として扱う



実際の計算：球形殻Eの重み付き和
球形殻E：球形準位の積分
重み：立体角(占有確率)の微分

核分裂(1)：核分裂障壁

Fission-barrier height is defined as **the highest saddle point** measured from the ground-state energy. (the saddle-point must be prolate)

$^{289}_{110}179$

(β -stable nucleus with the long $T_{\alpha}(\approx 1\text{yr})$)



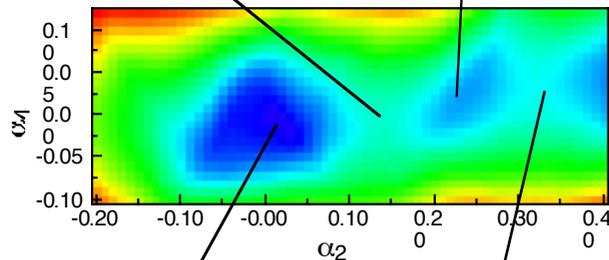
(Z, N)=(110, 179)
 $\alpha_2 = 0.14$
 $\alpha_4 = 0.01$
 $\alpha_6 = 0.024$



(Z, N)=(110, 179)
 $\alpha_2 = 0.24$
 $\alpha_4 = 0.02$
 $\alpha_6 = -0.009$

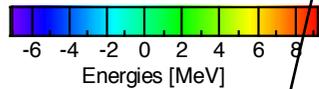
height: 4.74 MeV

Z=110, N=179 (free α_6 parameter)



→ Fission

shape: $\alpha_2, \alpha_4, \alpha_6$
 $(-0.2 \leq \alpha_2 \leq 0.5)$



(Z, N)=(110, 179)
 $\alpha_2 = 0.01$
 $\alpha_4 = 0.$
 $\alpha_6 = -0.001$

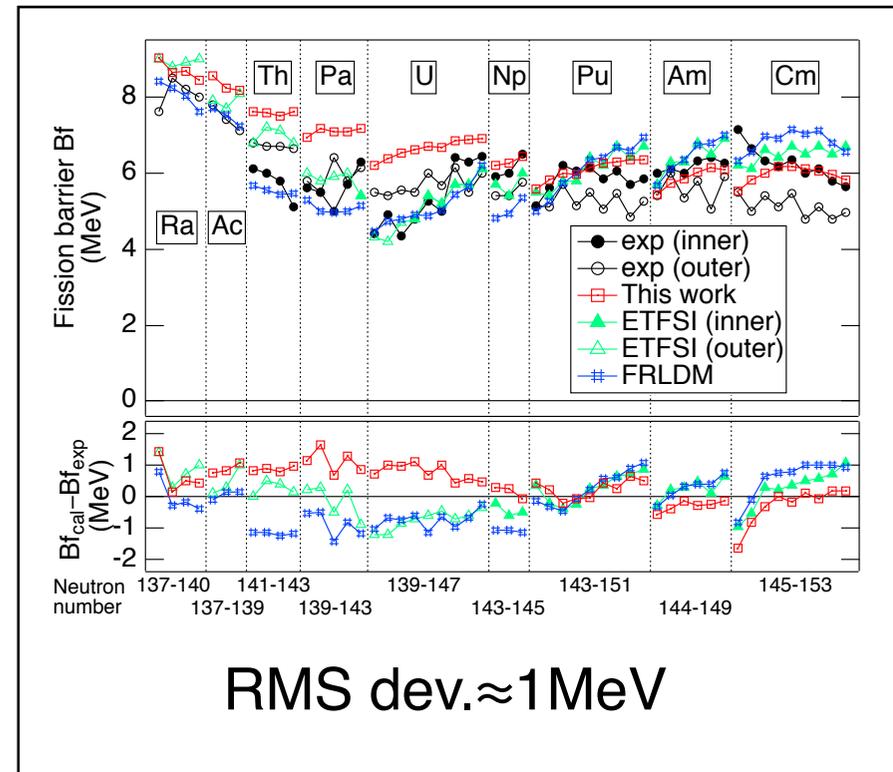


(Z, N)=(110, 179)
 $\alpha_2 = 0.32$
 $\alpha_4 = 0.03$
 $\alpha_6 = 0.002$

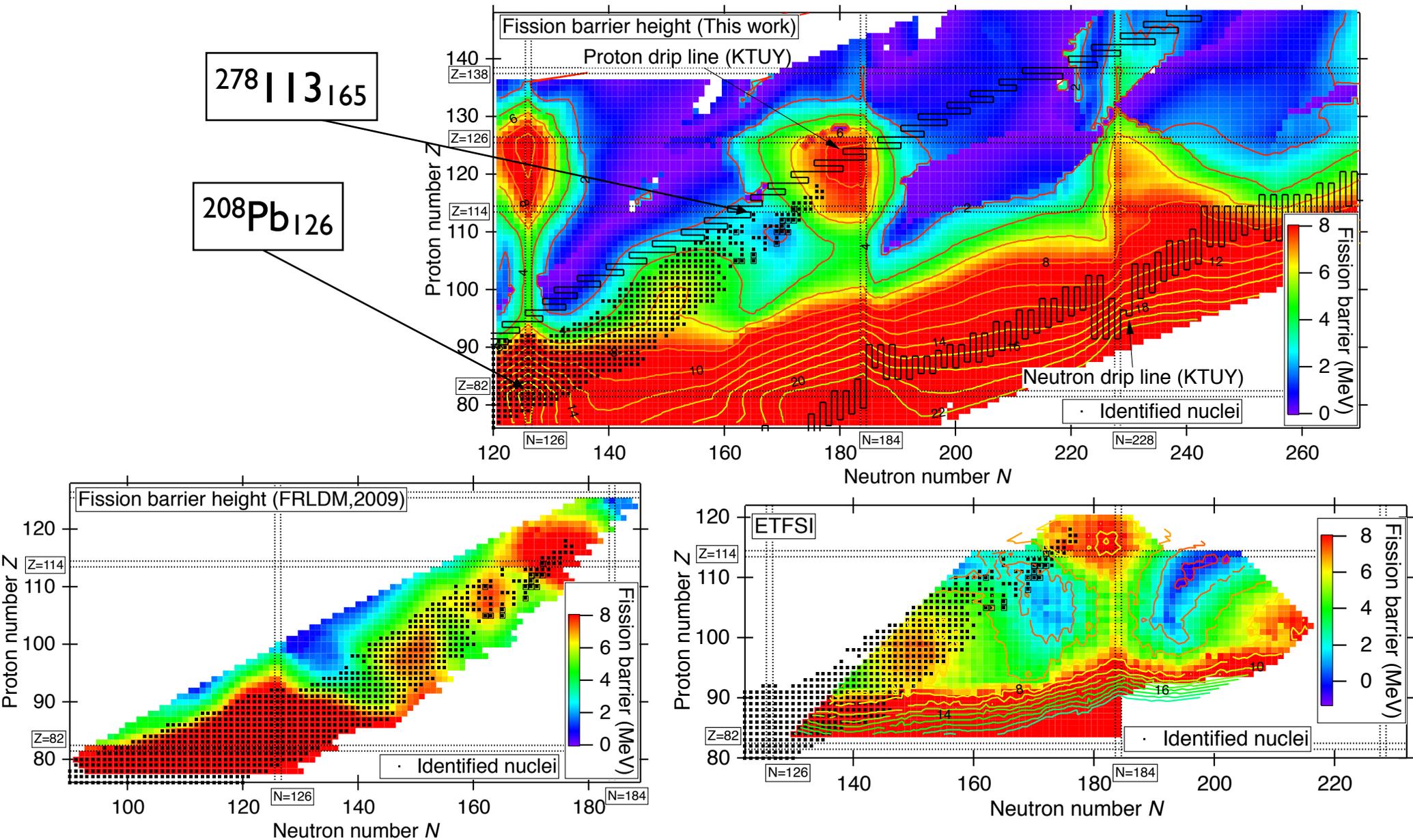
height: 4.11 MeV

ground state

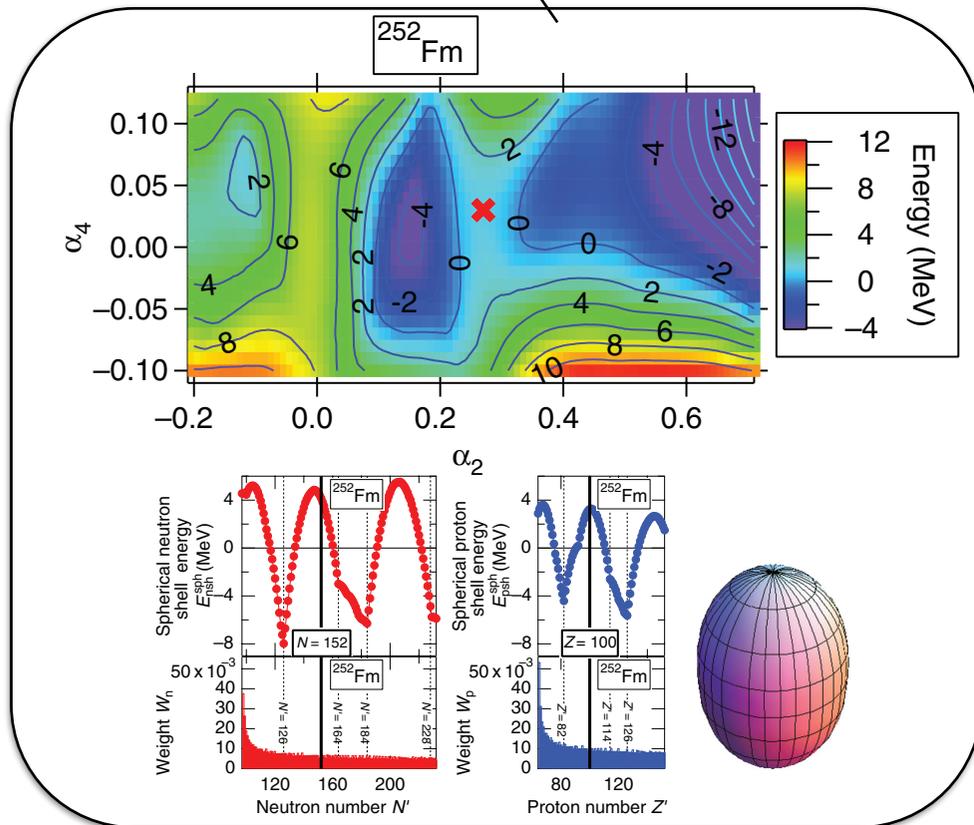
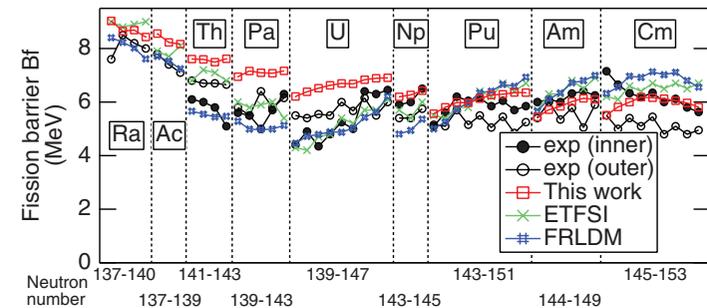
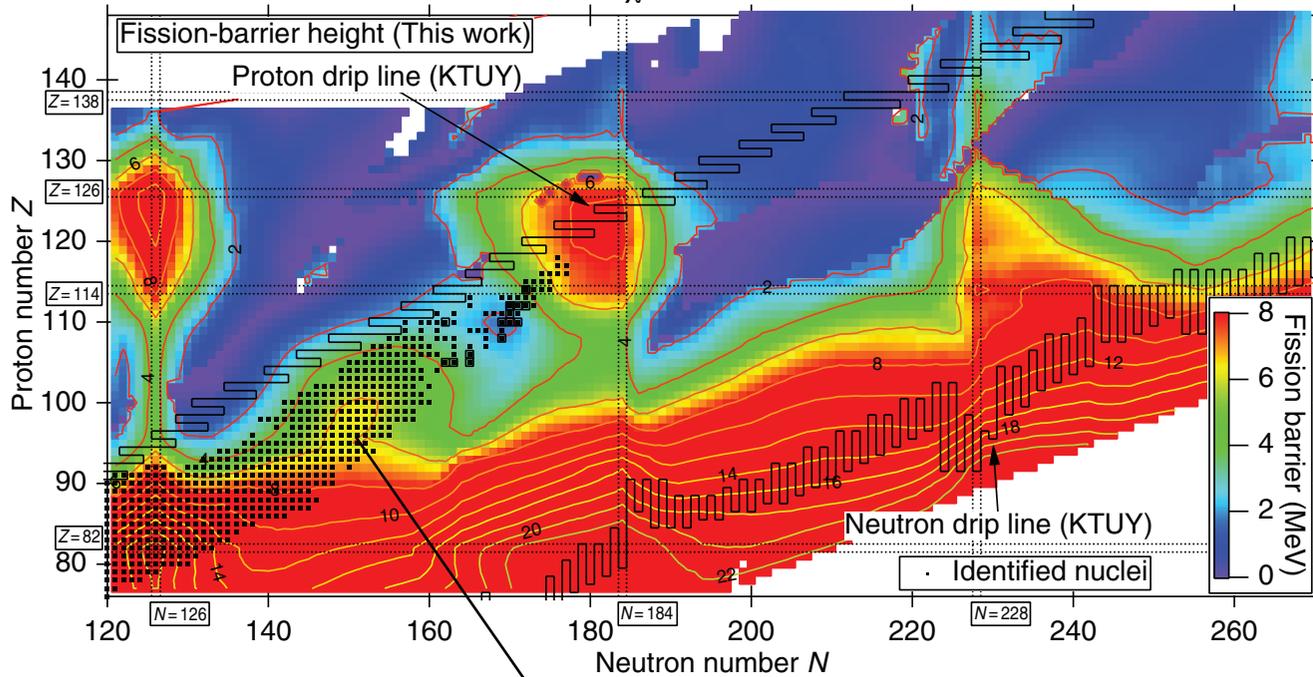
Energy surface (KUTY)



Fission barrier height

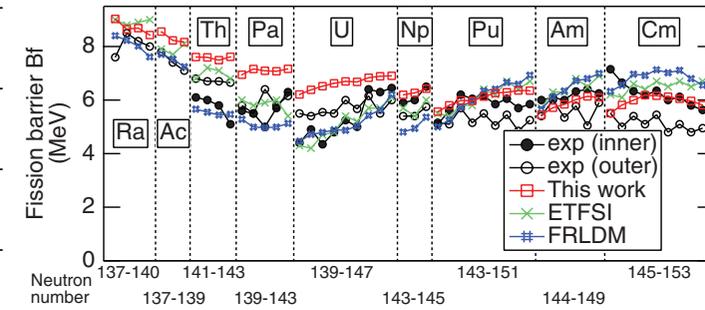
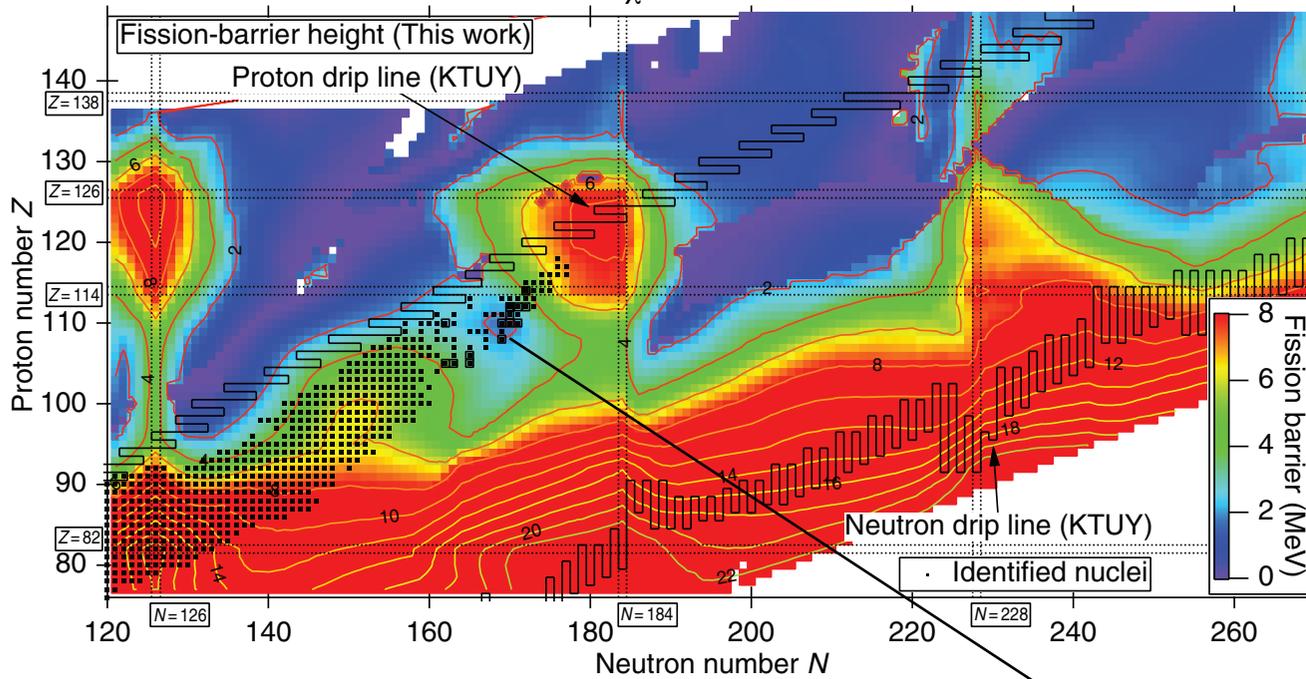


$$R(\theta) = \frac{R_0}{\lambda} [1 + \alpha_2 P_2(\cos \theta) + \alpha_4 P_4(\cos \theta) + \alpha_6 P_6(\cos \theta)],$$



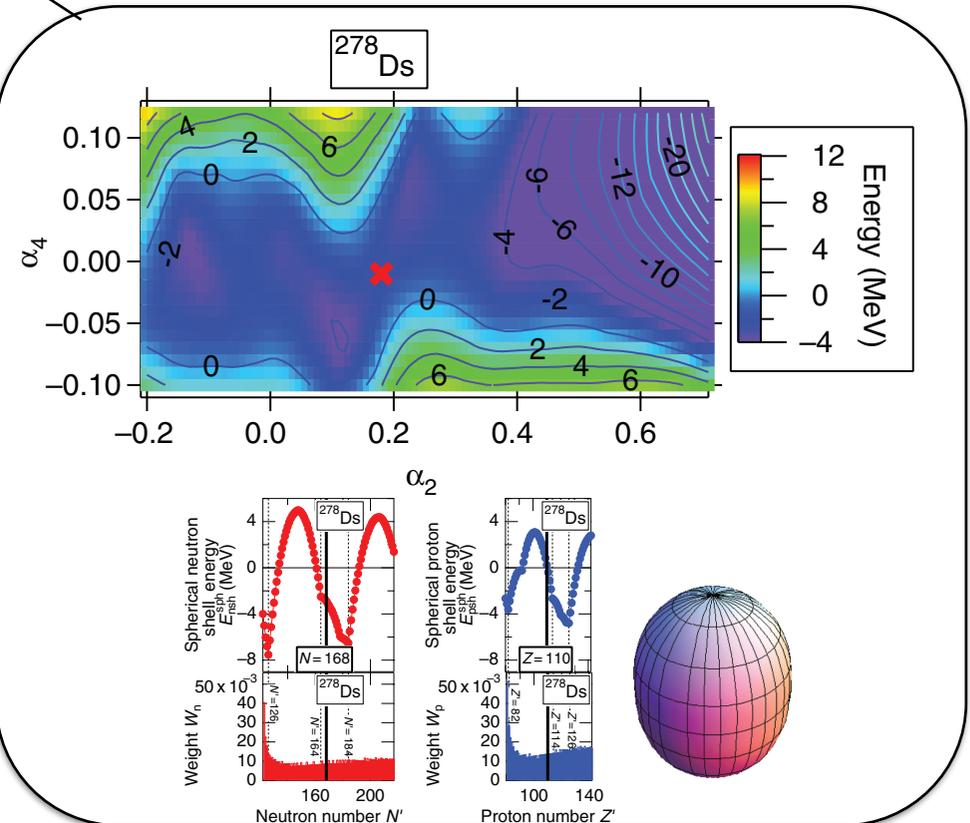
Neutron mixing weight reaches N=228 shell energy (left panel) : the saddle configuration of ^{252}Fm is contributed to by only one shell closure of N=228.

$$R(\theta) = \frac{R_0}{\lambda} [1 + \alpha_2 P_2(\cos \theta) + \alpha_4 P_4(\cos \theta) + \alpha_6 P_6(\cos \theta)],$$

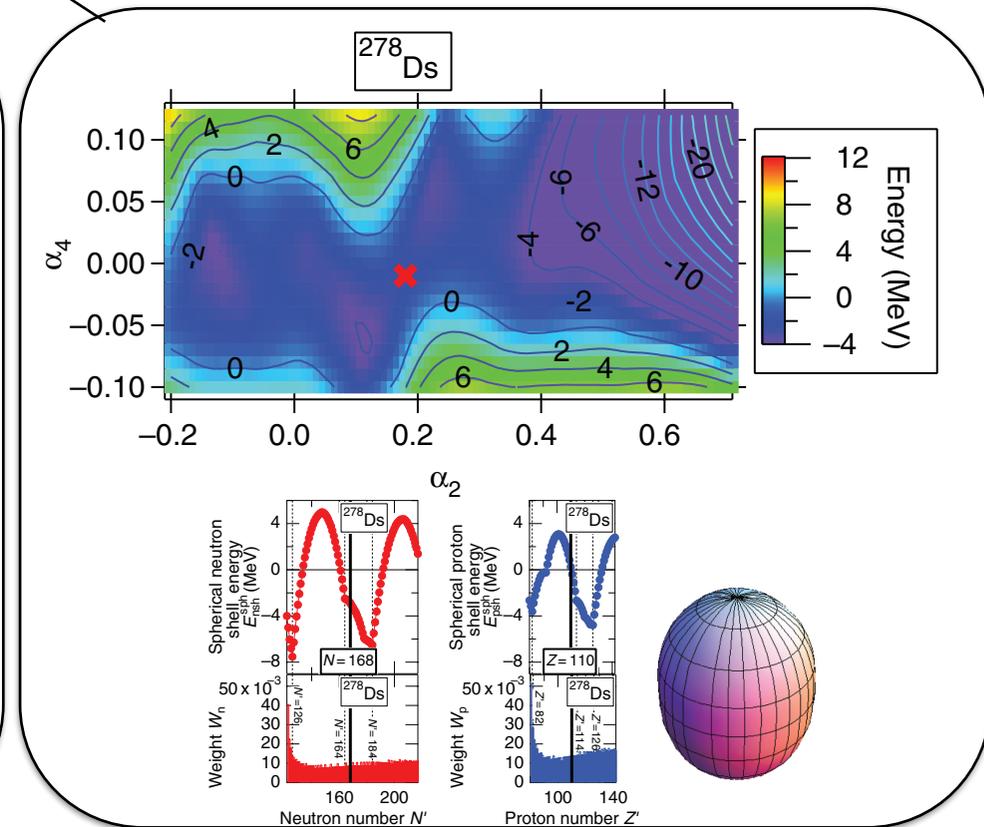
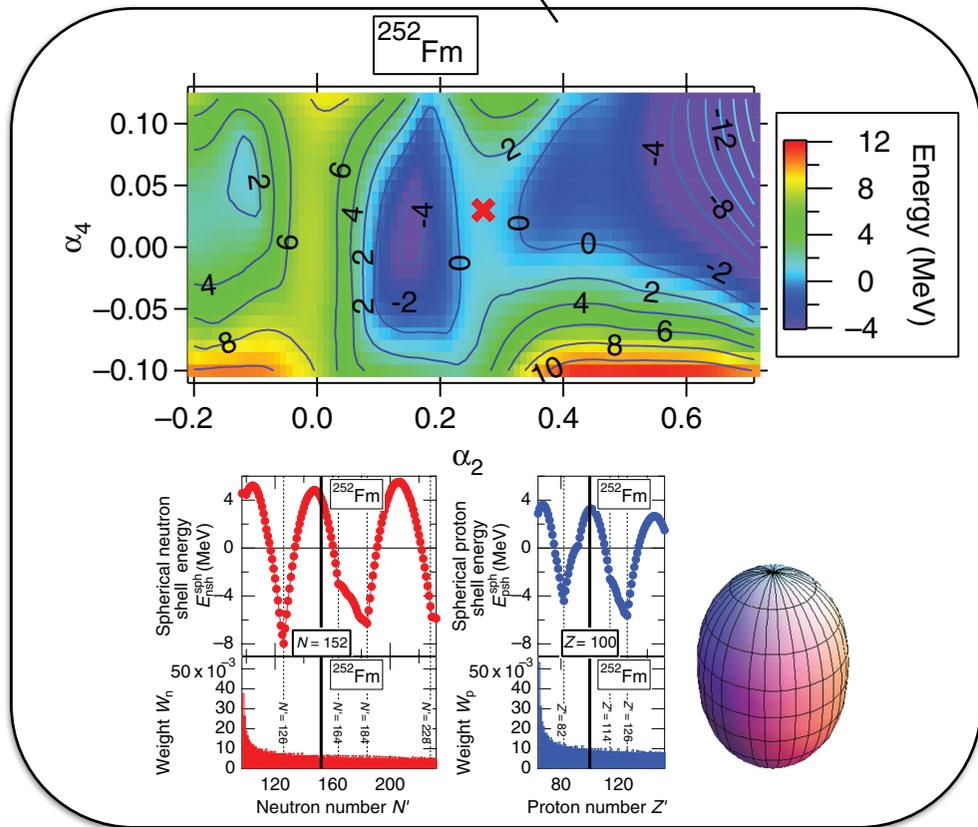
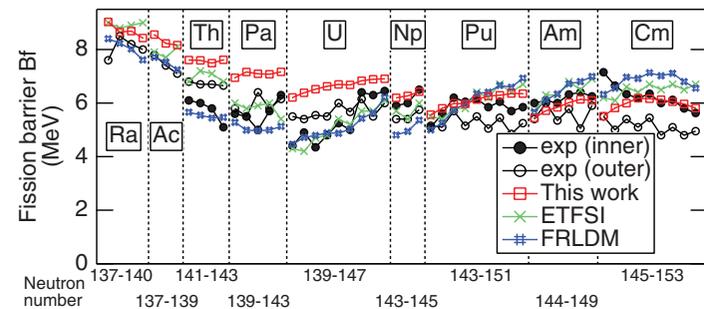
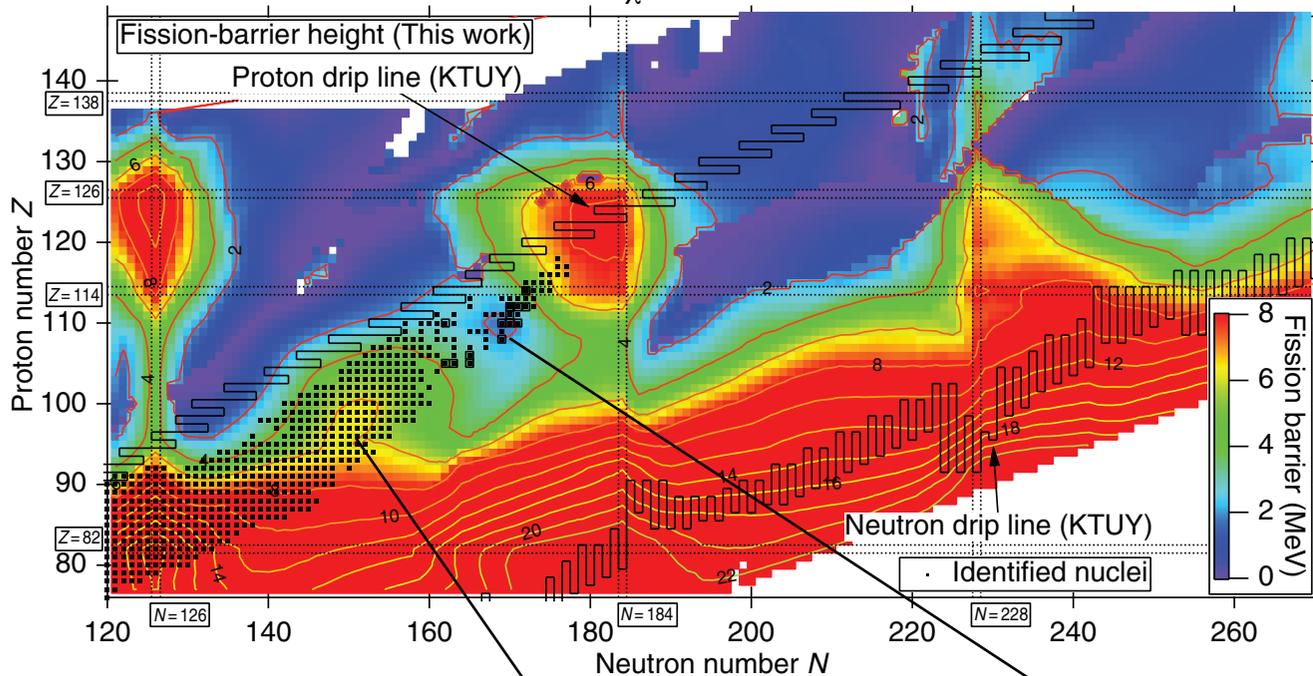


Neutron mixing weight reaches $N=126$ shell energy (left panel) and Proton mixing weight reaches $Z=82$ shell energy (right panel) : the saddle configuration of ^{278}Fm is contributed to by two shell closures of $Z=82$, $N=126$.

=> **^{208}Pb plus (collective) valence nucleons.**



$$R(\theta) = \frac{R_0}{\lambda} [1 + \alpha_2 P_2(\cos \theta) + \alpha_4 P_4(\cos \theta) + \alpha_6 P_6(\cos \theta)],$$



核分裂(2)：自発核分裂部分半減期の推定

- 原子核の形状: $\alpha_2, \alpha_4, \alpha_6$ (軸対称・反転対称)
- 1次元WKB法で透過確率を計算

$$\begin{aligned} \text{Log}_{10}(T_{\text{SF}}) = & \text{Log}_{10}\left(1 + \exp\left[\frac{2}{\hbar}K\right]\right) \\ & + \text{Log}_{10}(N_{\text{Coll}}) - 0.159 \\ & + h\delta_{\text{odd } Z} + h\delta_{\text{odd } N} - \Delta_{\text{oo}}\delta_{\text{odd } Z}\delta_{\text{odd } N} \end{aligned}$$

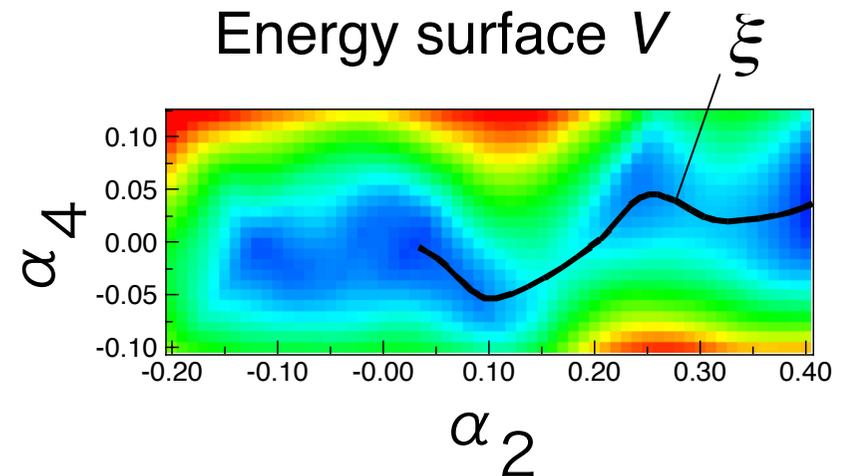
$$K = \int \sqrt{2M(V(\xi) - E_{\text{gs}})} d\xi$$

$$M = k\mu, \mu: \text{reduced mass}$$

$$d\xi = r_0 A^{1/3} d\alpha$$

$$r_0 = 1.2\text{fm}, \text{Log}_{10}(N_{\text{Coll}}) = 20.38$$

$$\delta_{\text{odd } Z} = \begin{cases} 0 & \text{for even-}Z \\ 1 & \text{for odd-}Z, \end{cases} \quad \delta_{\text{odd } N} = \begin{cases} 0 & \text{for even-}N \\ 1 & \text{for odd-}N, \end{cases}$$



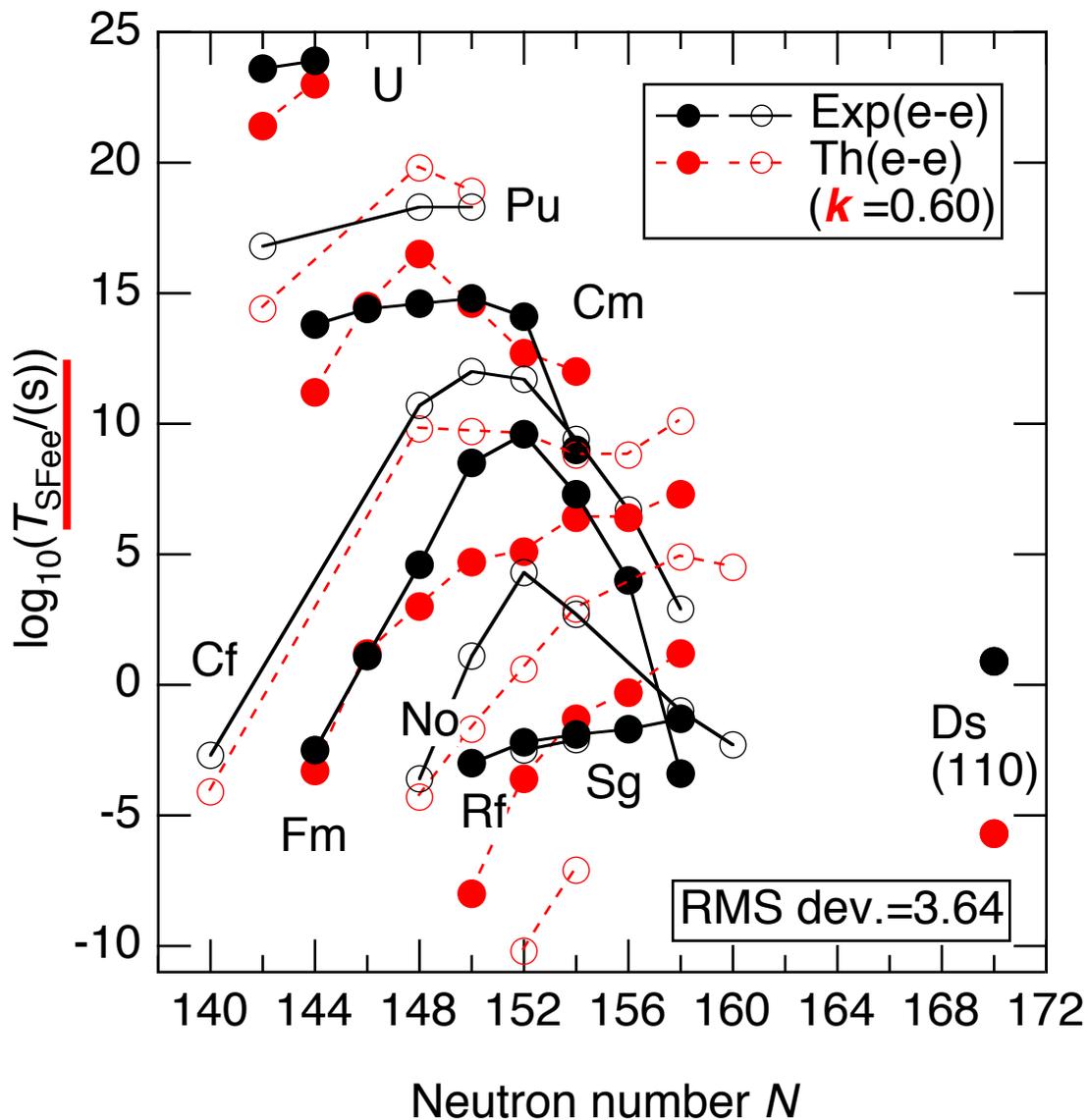
Adjustable parameter

k for e-e nuclei

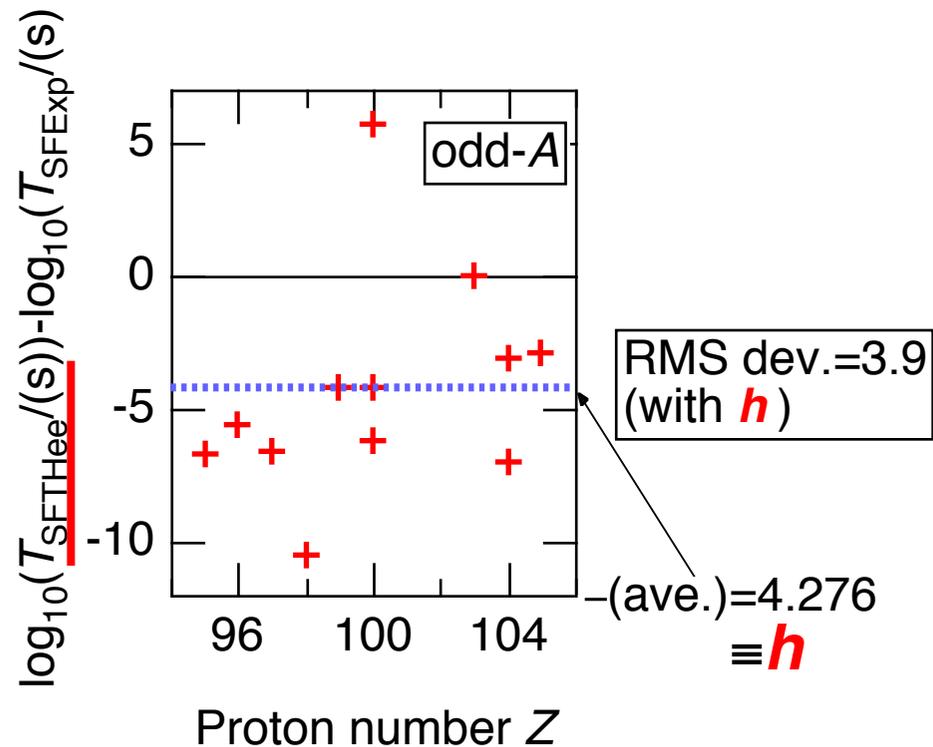
h, Δ_{oo} for odd-A, o-o nuclei

$T_{sf}(s)$ の実験値と計算値との比較

Even-even nuclei

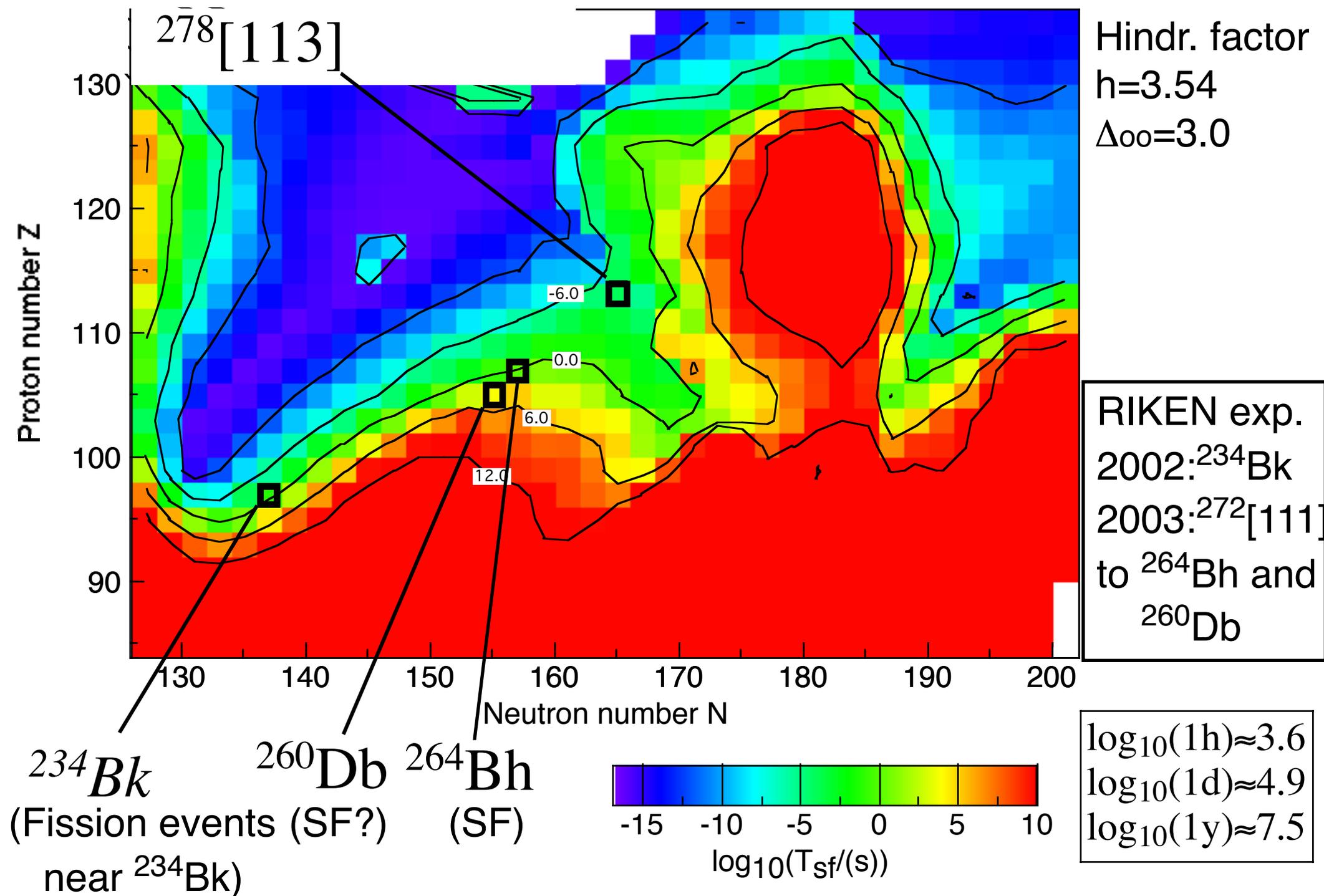


odd-A nuclei



odd-odd nuclei:
 o-o correction $-\Delta_{oo} = -2.83$
 is added

Calculated $\log_{10}(T_{sf}/(s))$ for odd-odd nuclei

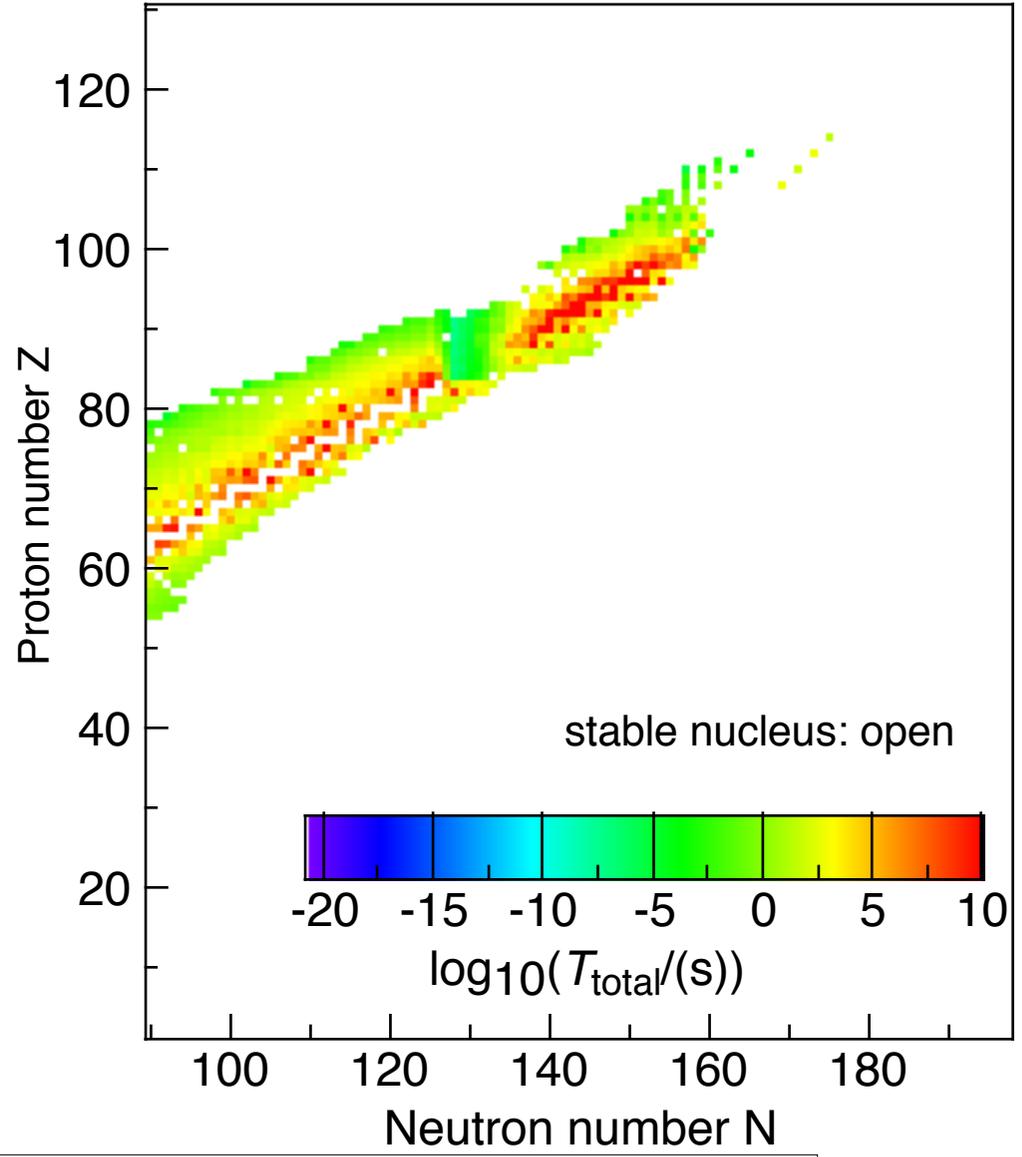
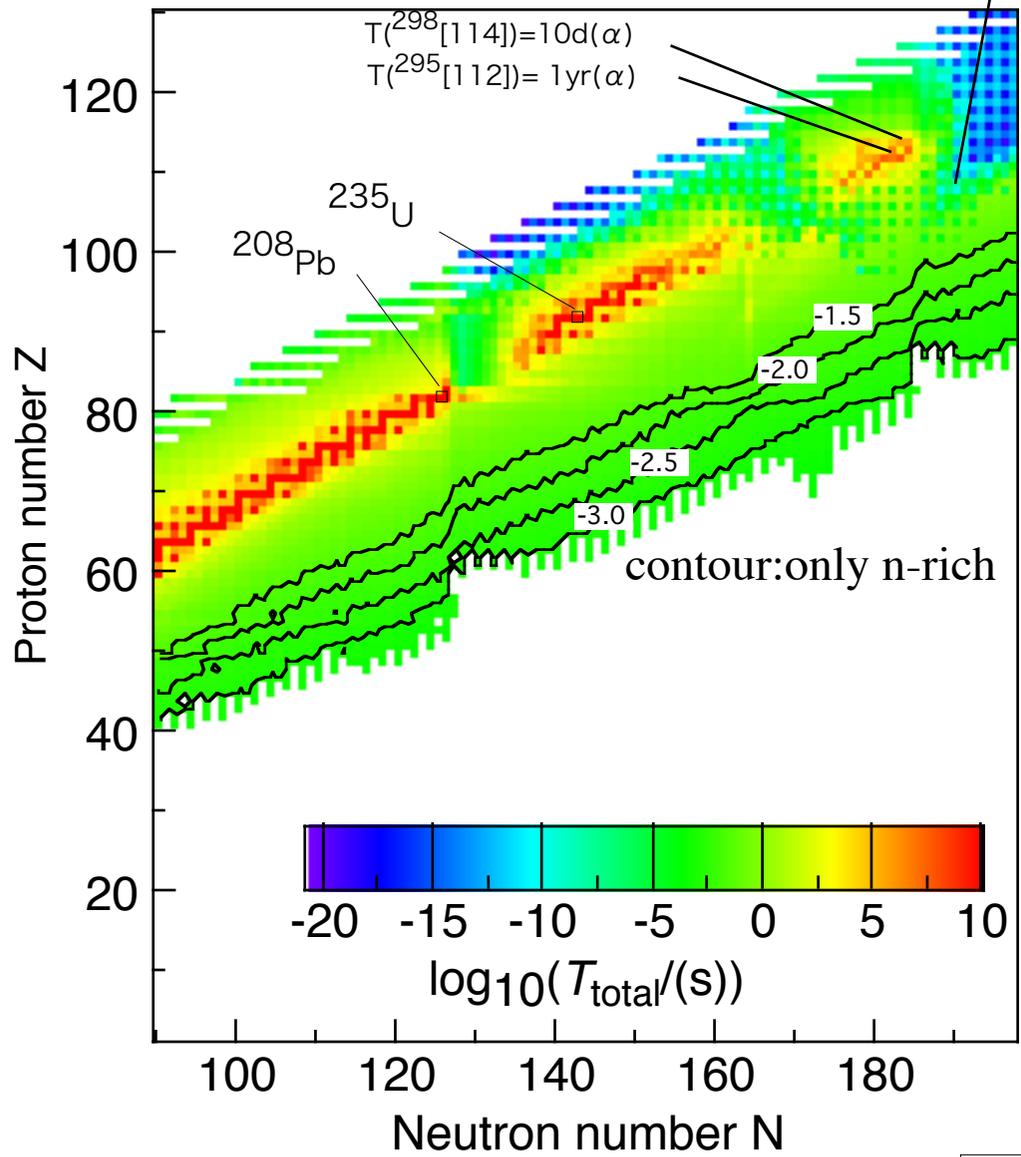


Total half lives(N≤200)

Log₁₀(T_{total}/(s)) (α, β, sf)

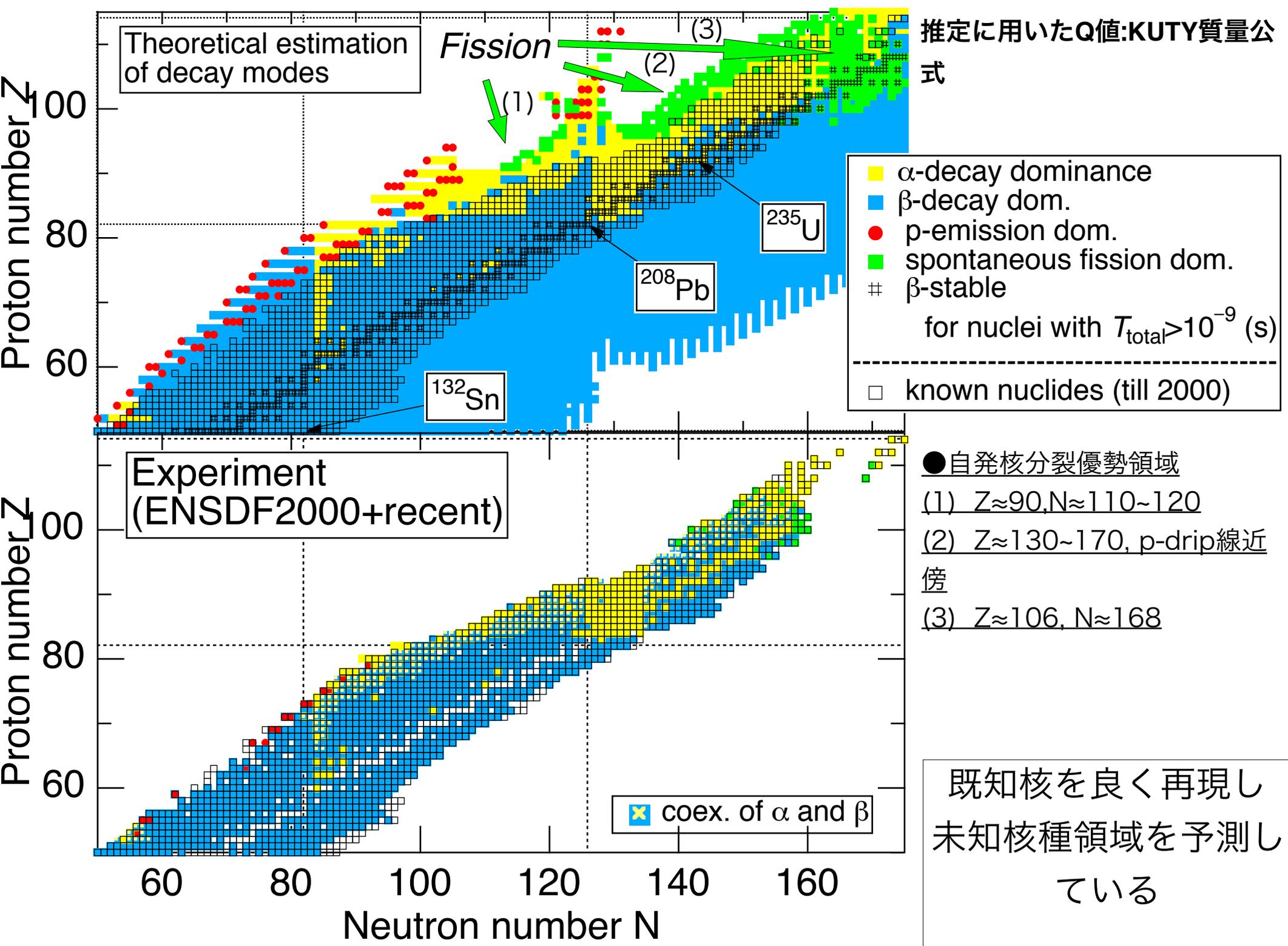
T(²⁹⁸Hs)=10⁻¹⁰s

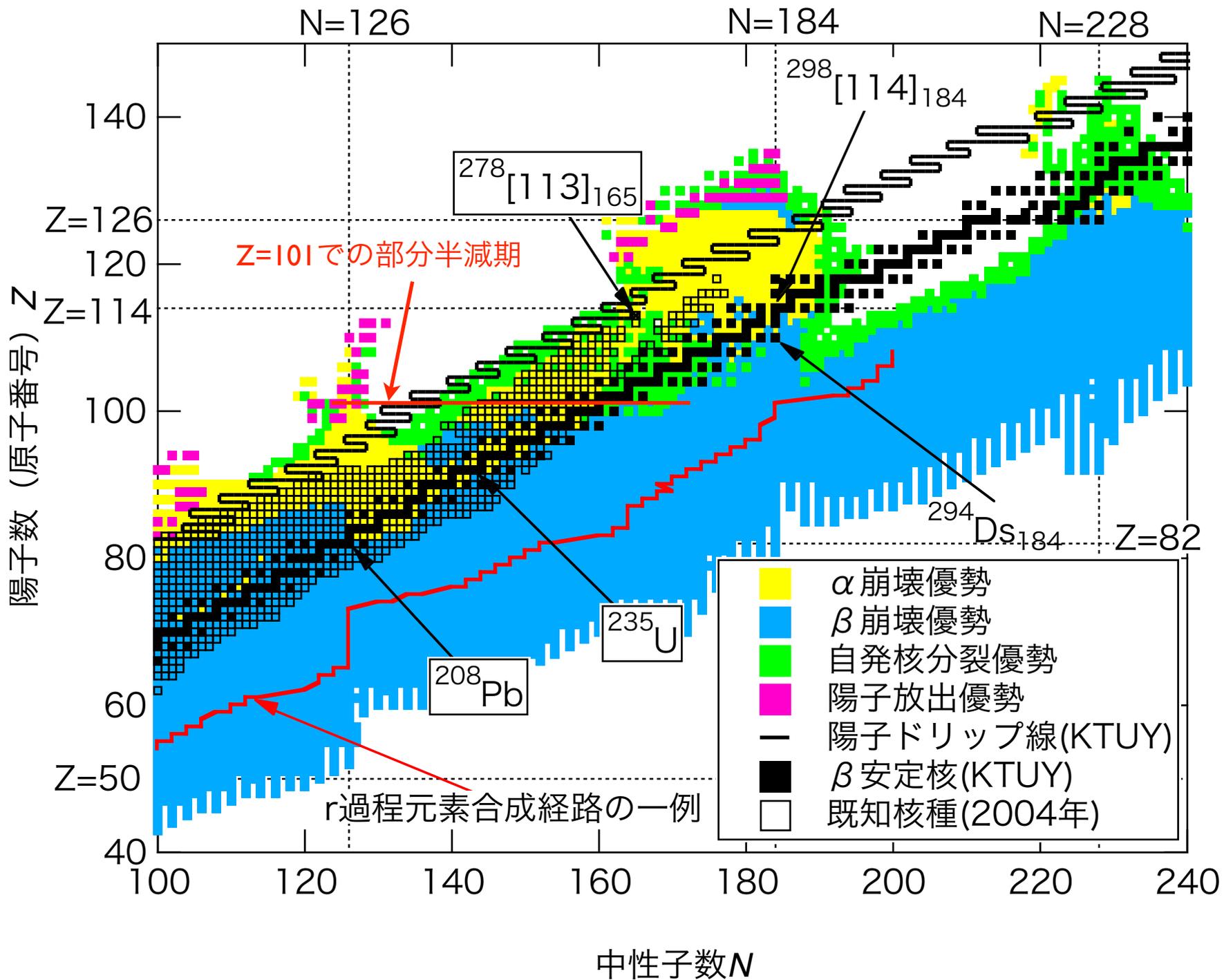
Log₁₀(T_{exp}/(s)) (ENSDF2000, August)



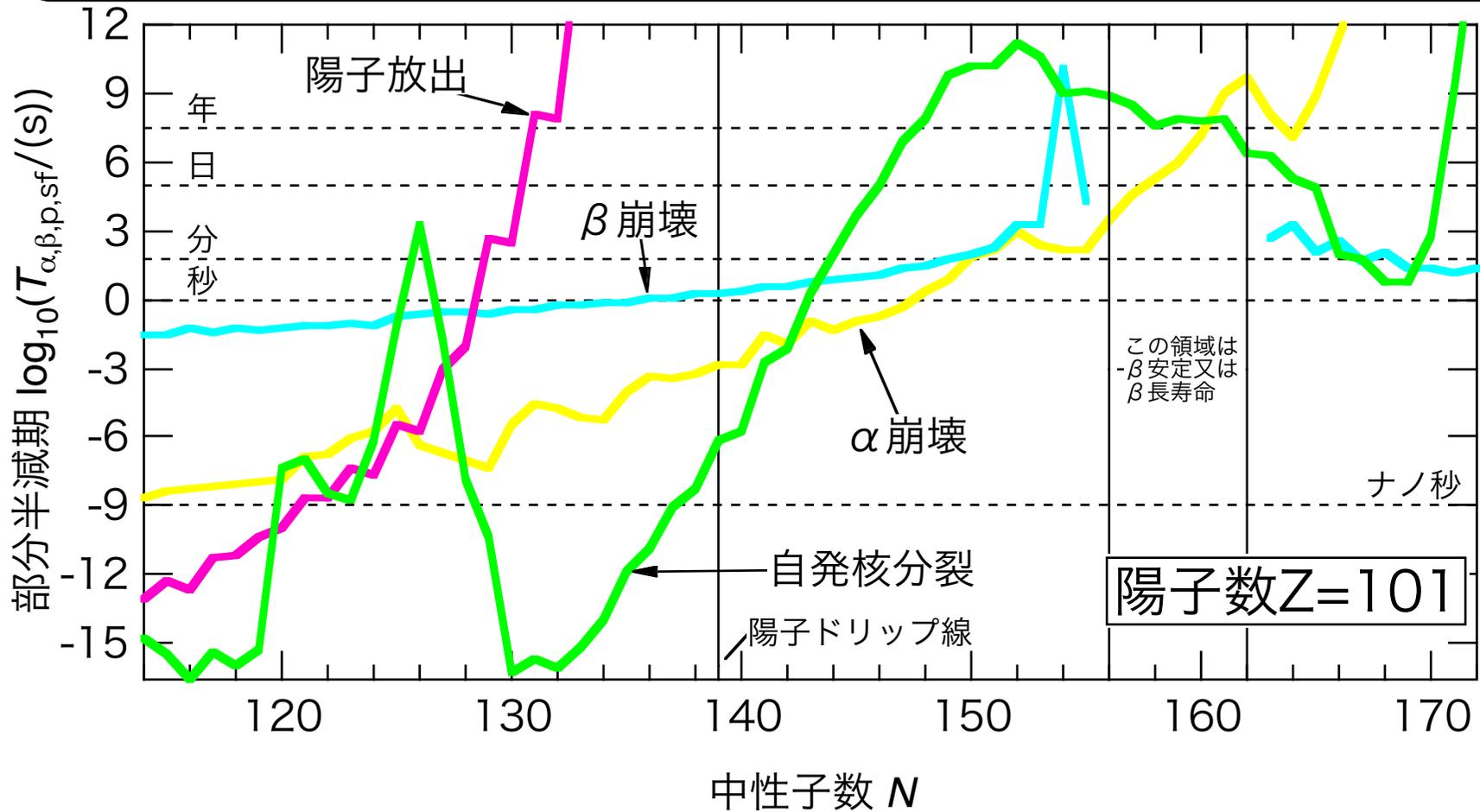
$$\frac{1}{T_{\text{total}}} = \frac{1}{T_{\alpha}} + \frac{1}{T_{\beta}} + \frac{1}{T_{\text{sf}}}$$

既知核を良く再現し未知核種領域を予測している





各崩壊の部分半減期



陽子放出: 陽子ドリップ線の(かなり)外から有意な寿命. かなり急変化.

α 崩壊:

β 崩壊: 1ms程度以上をなだらかに推移. $N=154-162$ 付近で長寿命or β 安定.

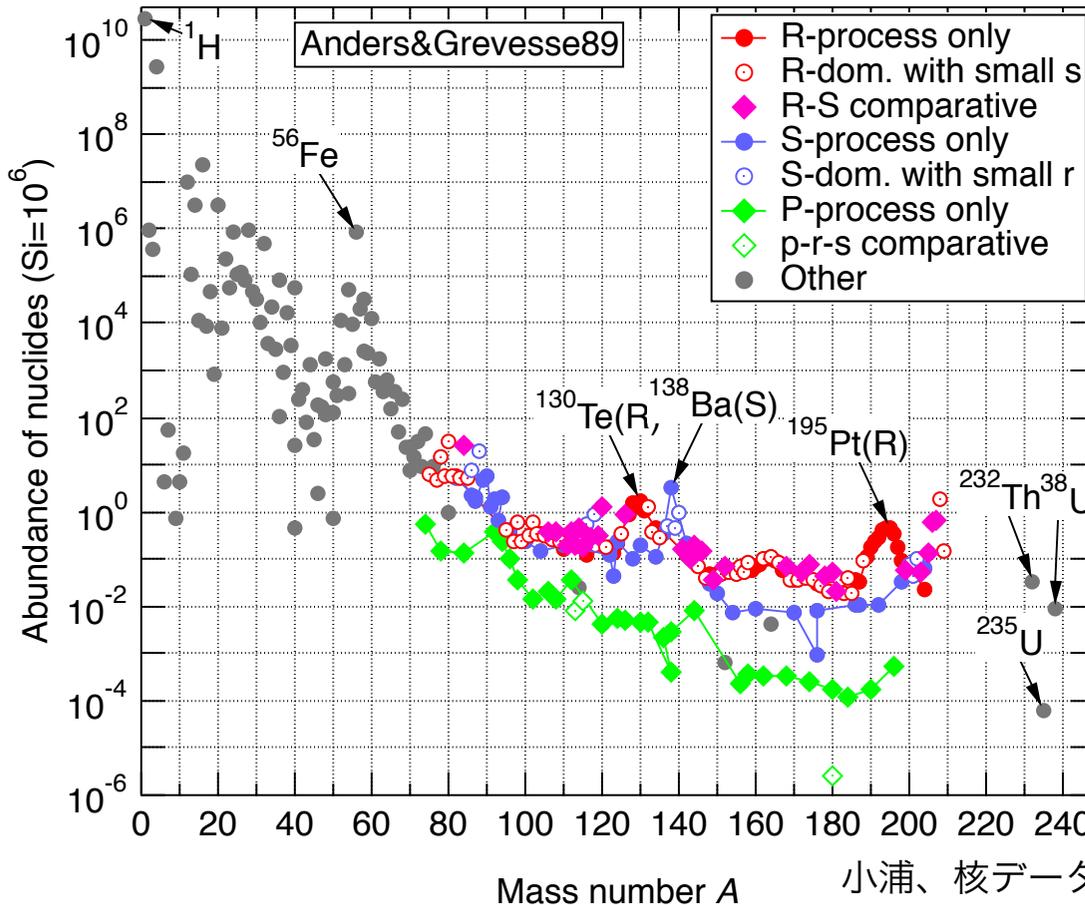
自発核分裂: 核子数依存性が大きい (閉殻およびその中間領域が長寿命)

自発核分裂、陽子放出 \gg α 崩壊 \gg ベータ崩壊



r-process nucleosynthesis

原子核の起源の理論的探求：星の元素合成



- **S-process:** 遅中性子捕獲過程。
赤色巨星などで数千年程度かけて中性子捕獲反応が進む。
- **R-process:** 速中性子捕獲過程。
超新星爆発などで数秒で中性子捕獲反応が進む。

太陽系における同位体の存在比（観測値）

鉄(Fe)より重い原子核の現在の理解

- **Fe-Bi**：赤色巨星によって作られた(s過程(slow process))
- **Fe-U**：超新星爆発によって作られた(r過程(rapid process))

太陽系における同位体の存在比

水素・ヘリウム
(多い)

縦軸は陽子の数

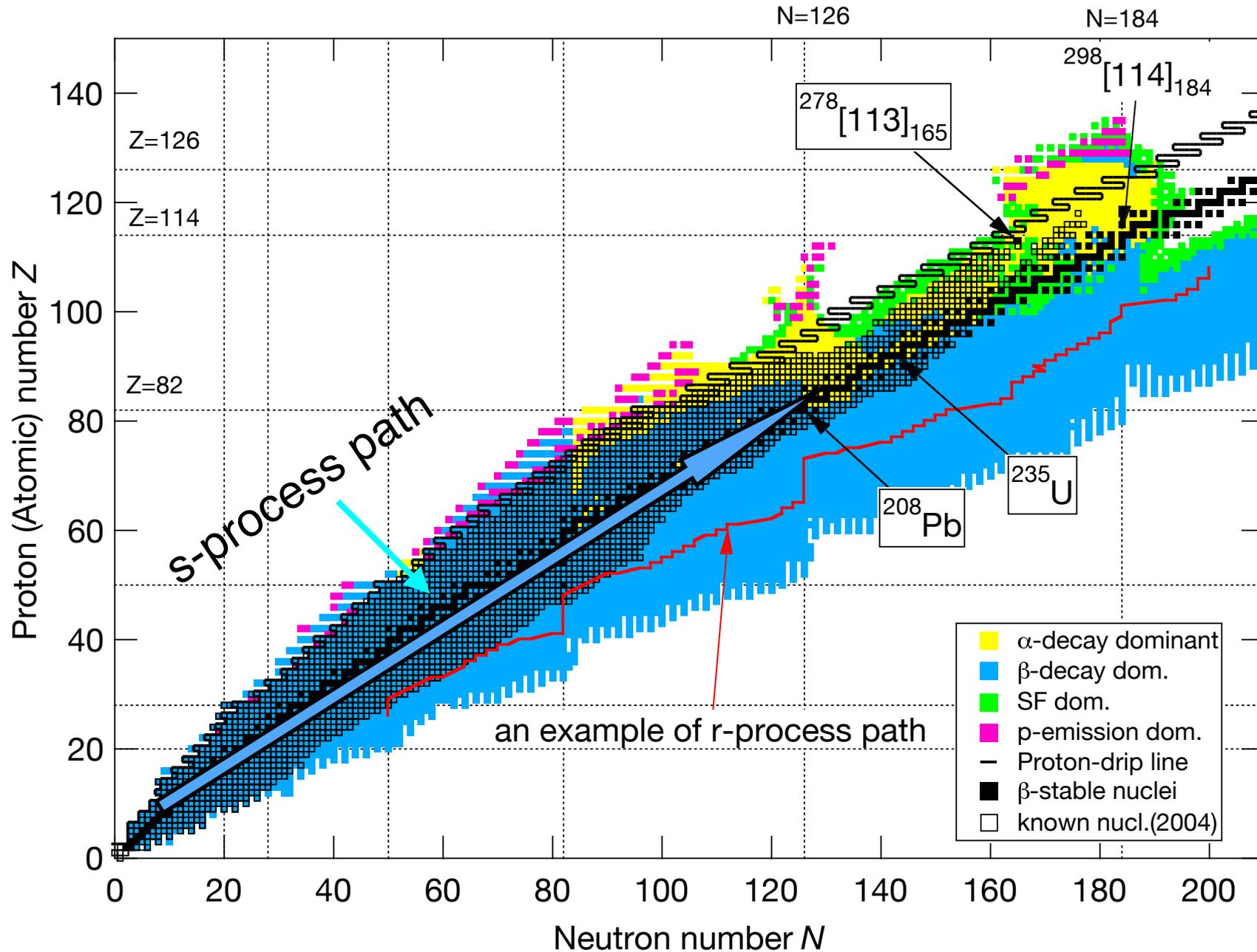
トリウム、ウラン
(孤立している)

^{56}Fe 付近
(周りに比べて多い)

横軸は中性子の数

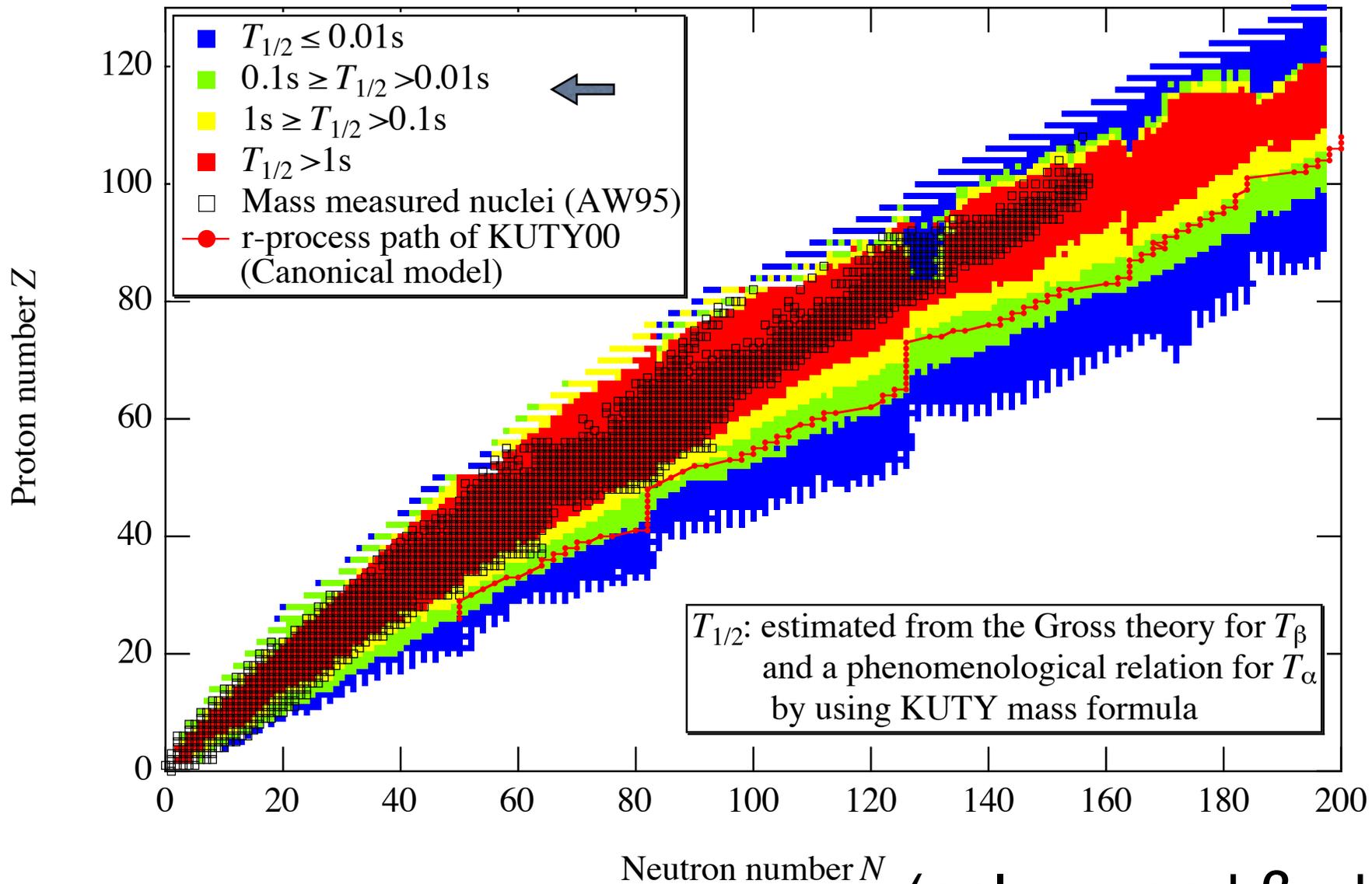
なぜこのような存在比となっているのだろうか？

s- and r-process path



Calculated by the KTUY formula

α 崩壊と β 崩壊を考慮した半減期計算値



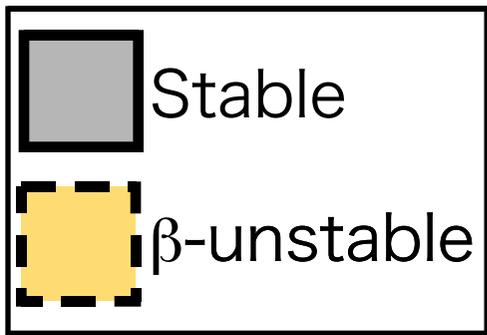
(only α - and β - decay)

r過程経路核 : 0.1-0.01s

r過程後 β 崩壊核 : 0.1s-

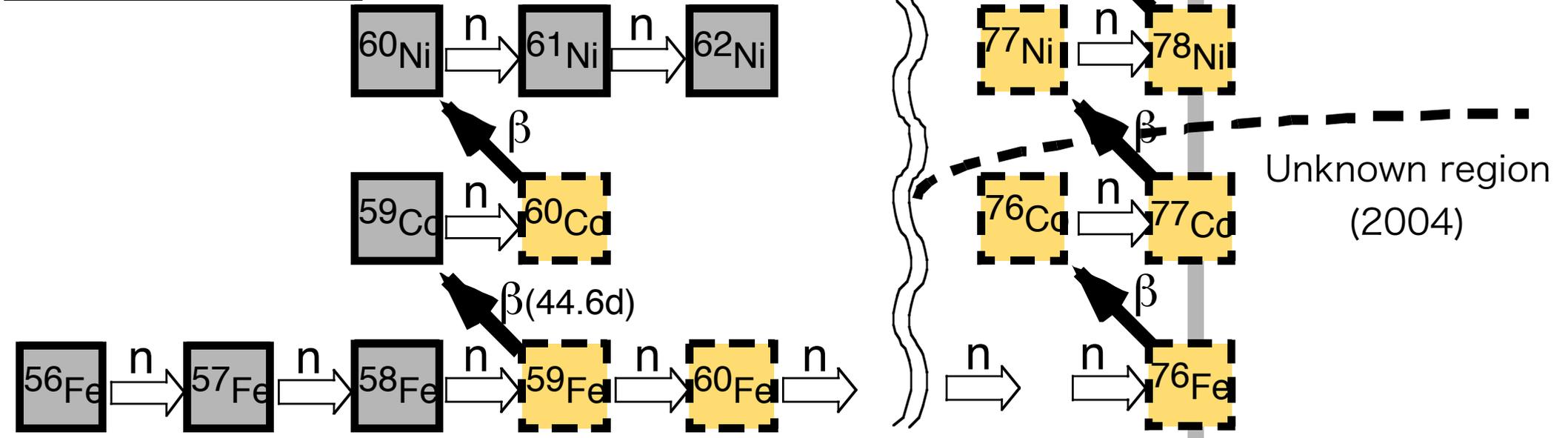
$$\frac{1}{T_{1/2}} = \frac{1}{T_{\alpha}} + \frac{1}{T_{\beta}}$$

S- and R-process path from ^{56}Fe regarded as a seed nucleus



s-process

r-process



^{56}Fe (seed)

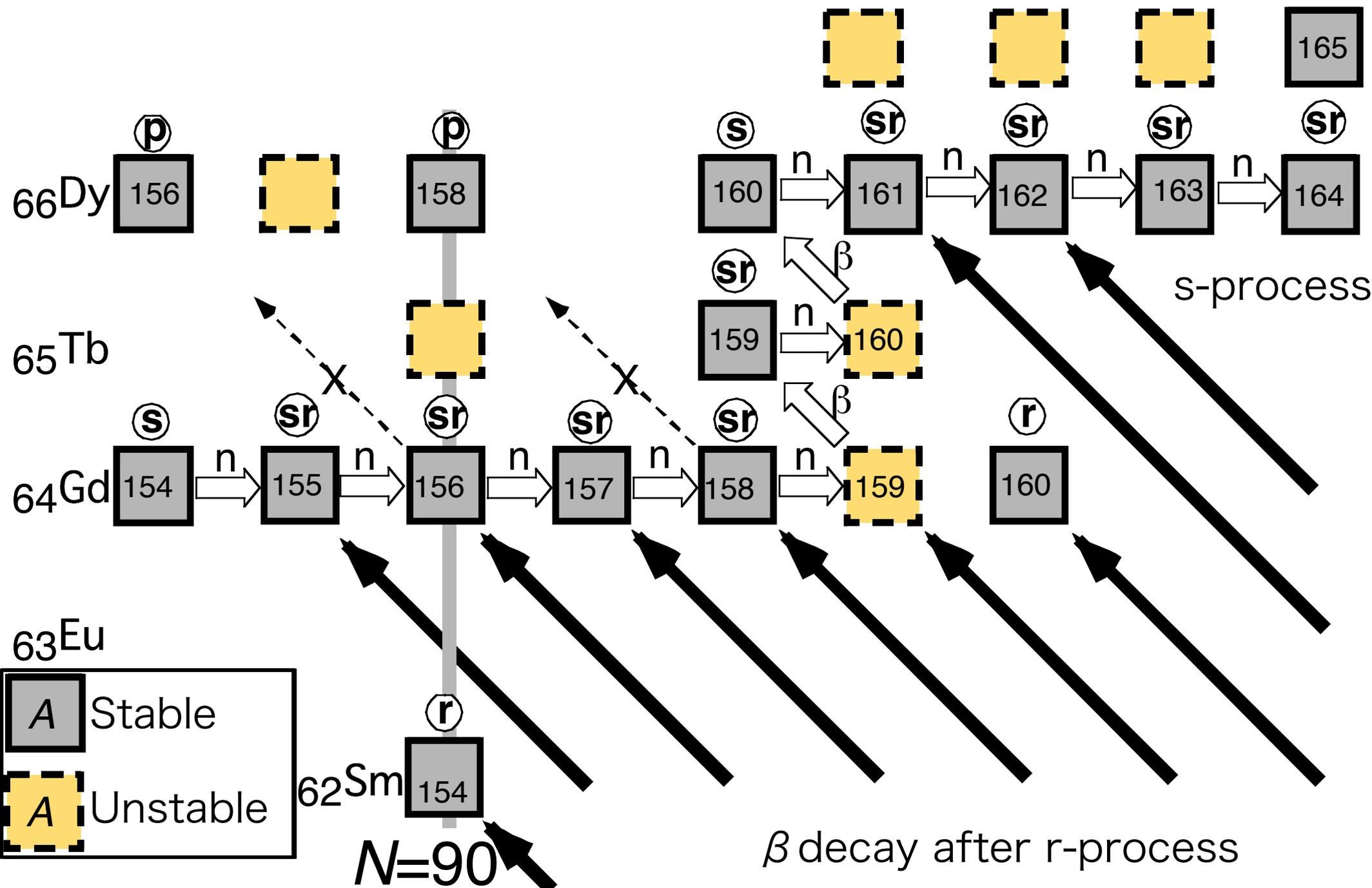
$\lambda_n \ll \lambda_\beta \Rightarrow$ s-process
 $\lambda_n \gg \lambda_\beta \Rightarrow$ r-process

$N=50$
 (Magic number, λ_n is small)

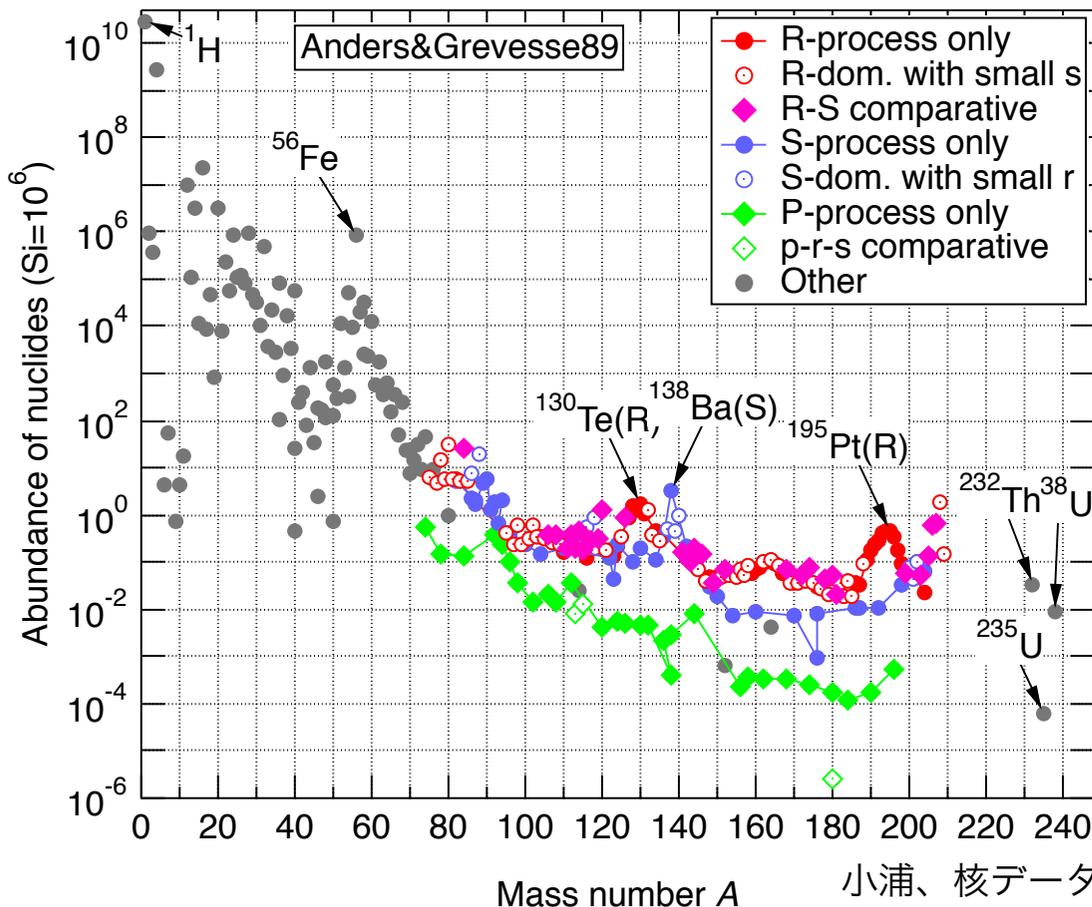
$\lambda_\beta = \ln 2 / T_{\beta 1/2}$
 $\lambda_n = N_n v_T \langle \sigma \rangle$
 number density | thermal velocity at T | Maxwell-averaged cross section

ex. ^{59}Fe ($v_T \langle \sigma \rangle (^{59}\text{Fe}) = 3 \times 10^{-18} \text{cm}^3/\text{s}$)
 $N_n = 10^6 \text{cm}^{-3} \Rightarrow \lambda_n = 3 \times 10^{-12} \text{s}^{-1} \ll \lambda_\beta \Rightarrow$ s-process
 $N_n = 10^{20} \text{cm}^{-3} \Rightarrow \lambda_n = 3 \times 10^2 \text{s}^{-1} \gg \lambda_\beta \Rightarrow$ r-process

s- and r-process nuclei



目的：原子核の起源の理論的探求 一星の元素合成一



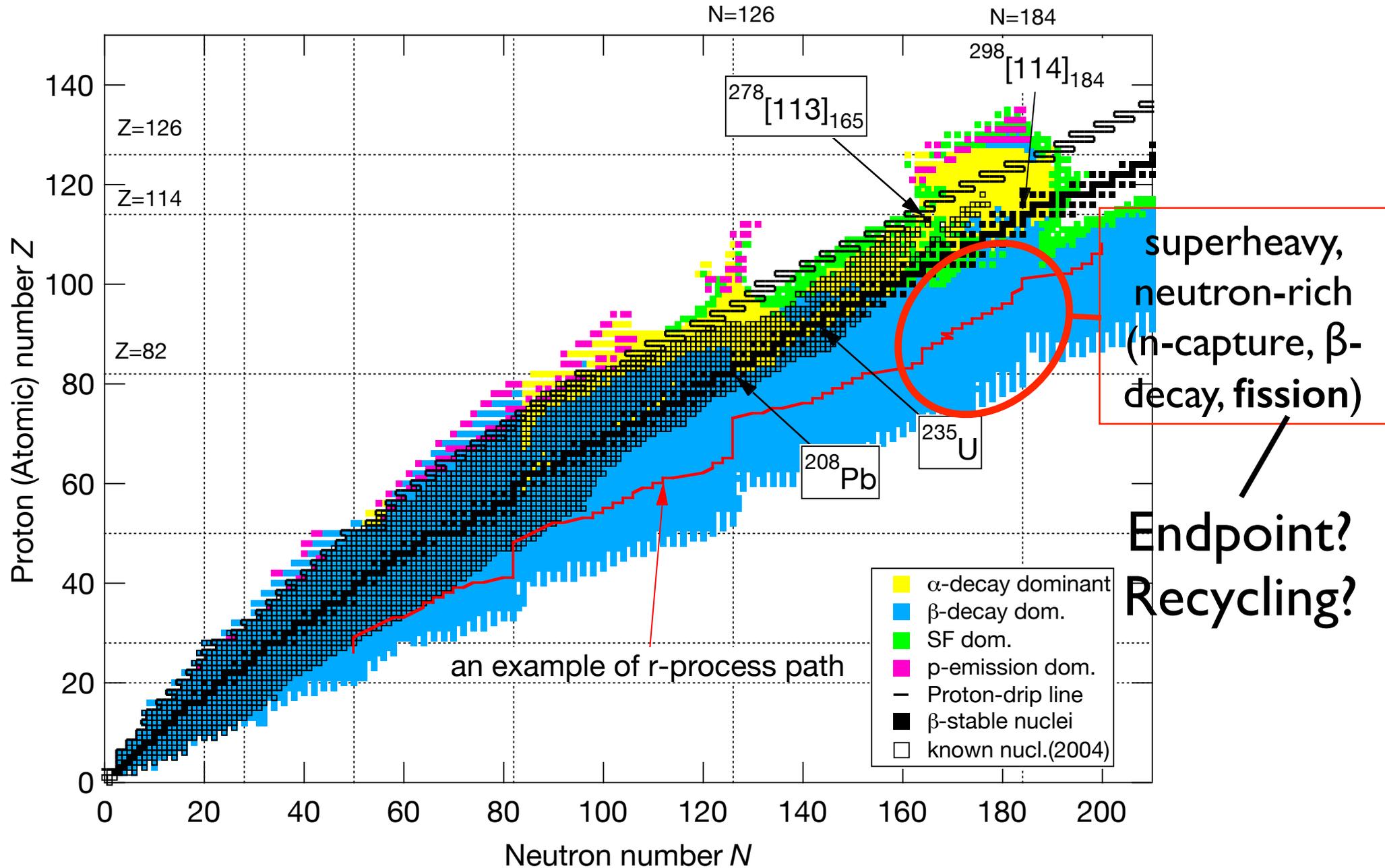
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r-process region



Calculated by the KTUY formula



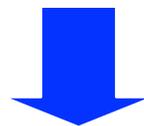
r-process nucleosynthesis and nuclear fission

I. Fission Fragment mass distribution

Potential Energy Surface (PES)

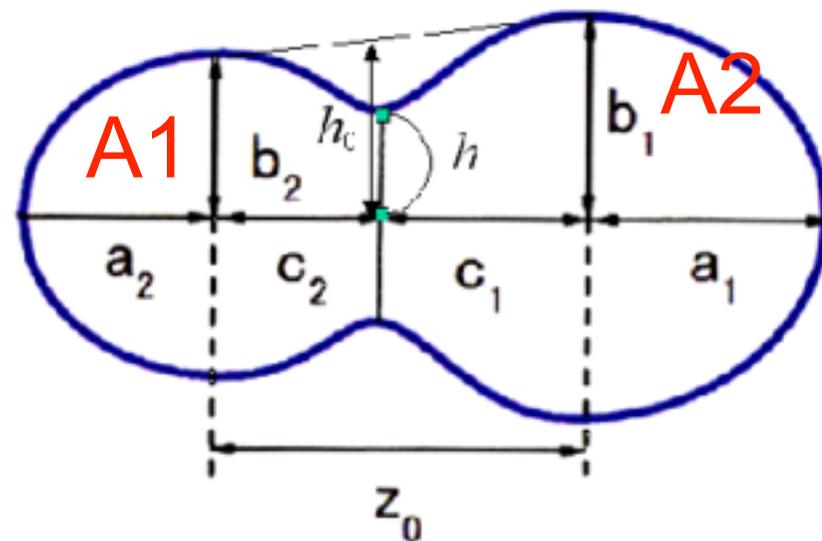
Liquid-drop model + Two-center shell model

Code:Yamaji-Iwamoto (70)



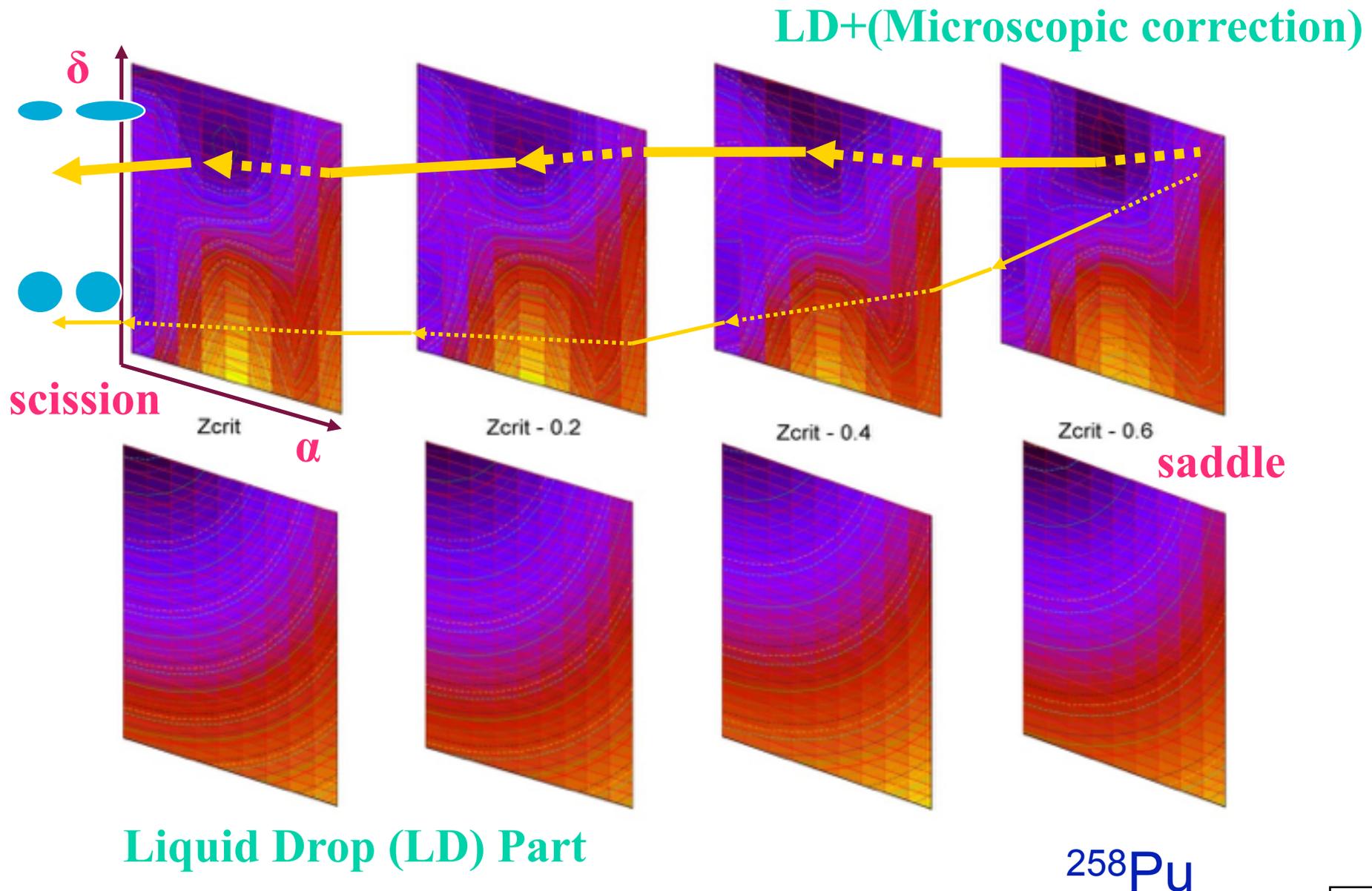
PES: 3-dim. deformation parameter space

- Center-of-mass distance: $Z = \frac{Z_0}{BR}$
- Deformation of fragment: $\delta = \frac{3(a-b)}{2a+b}$
- Mass asymmetry: $\alpha = \frac{A_1 - A_2}{A_1 + A_2}$



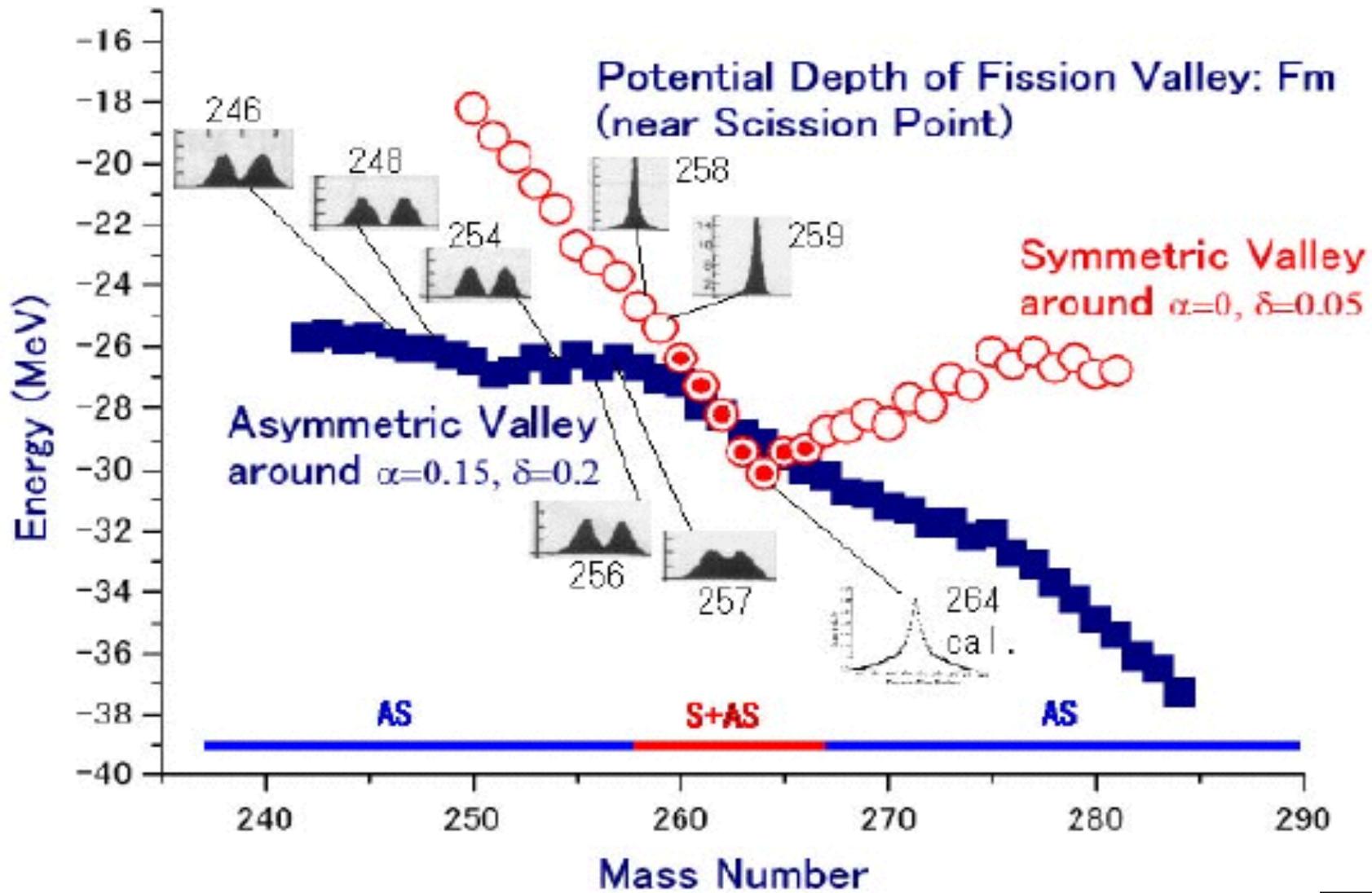
$$\left[B = \frac{3 + \delta}{3 - 2\delta}, \quad R : \text{Radius of the spherical compound nucleus} \right]$$

Path of fragments in the 3-dim. deformation space



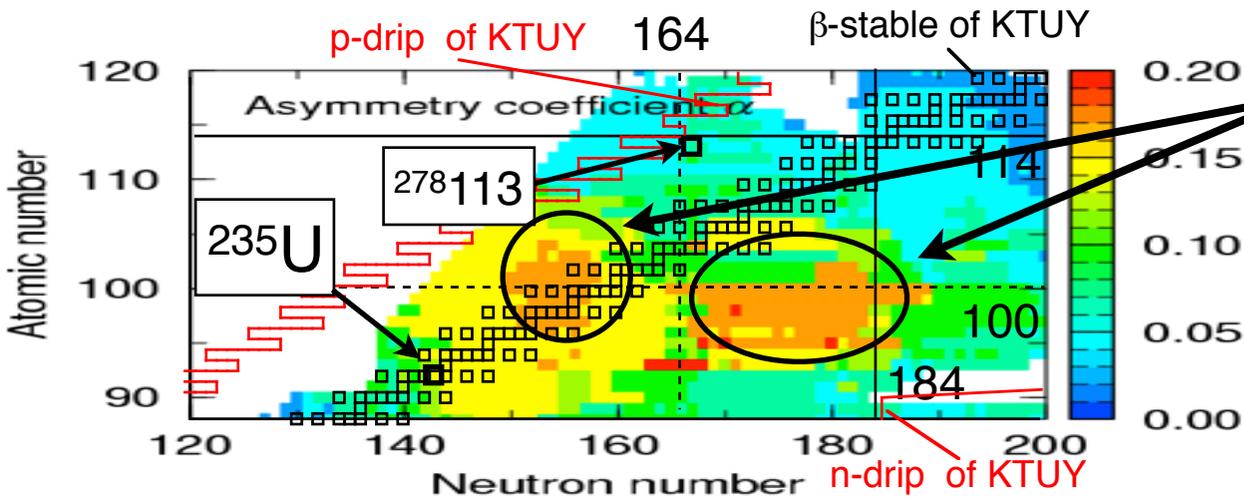
Region of Symmetric/Asymmetric fission

Analysis of PES near Scission Point for Fm isotopes



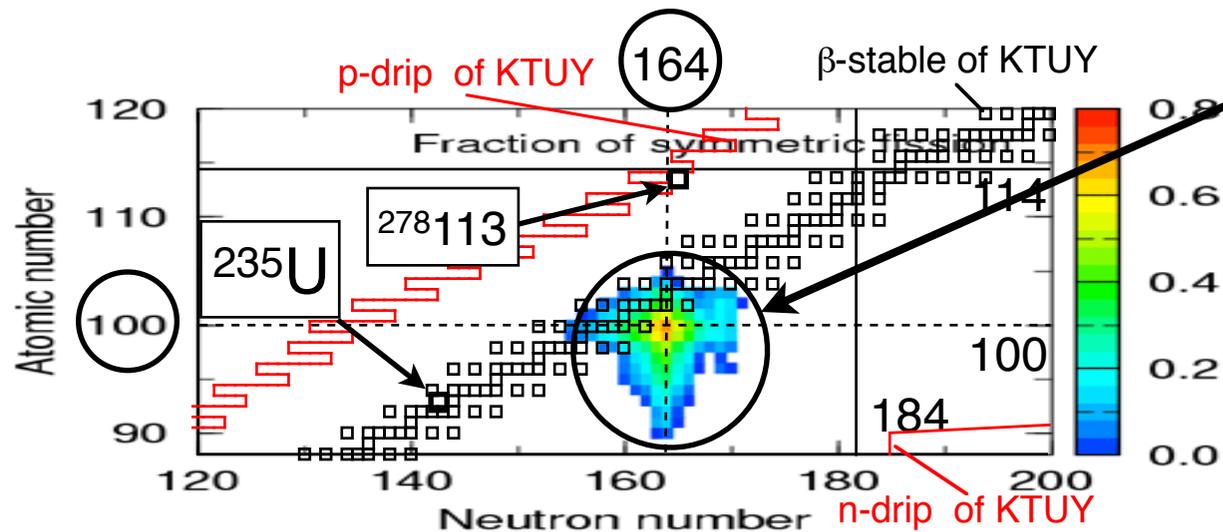
Result - Asymmetric parameter

Asymmetric coefficient α



Well-asymmetric region:
 Located around ^{254}Fm
 ($Z=100, N=154$) and ^{264}Cf
 ($Z=98, N=176$)

Fraction of Symmetric fission

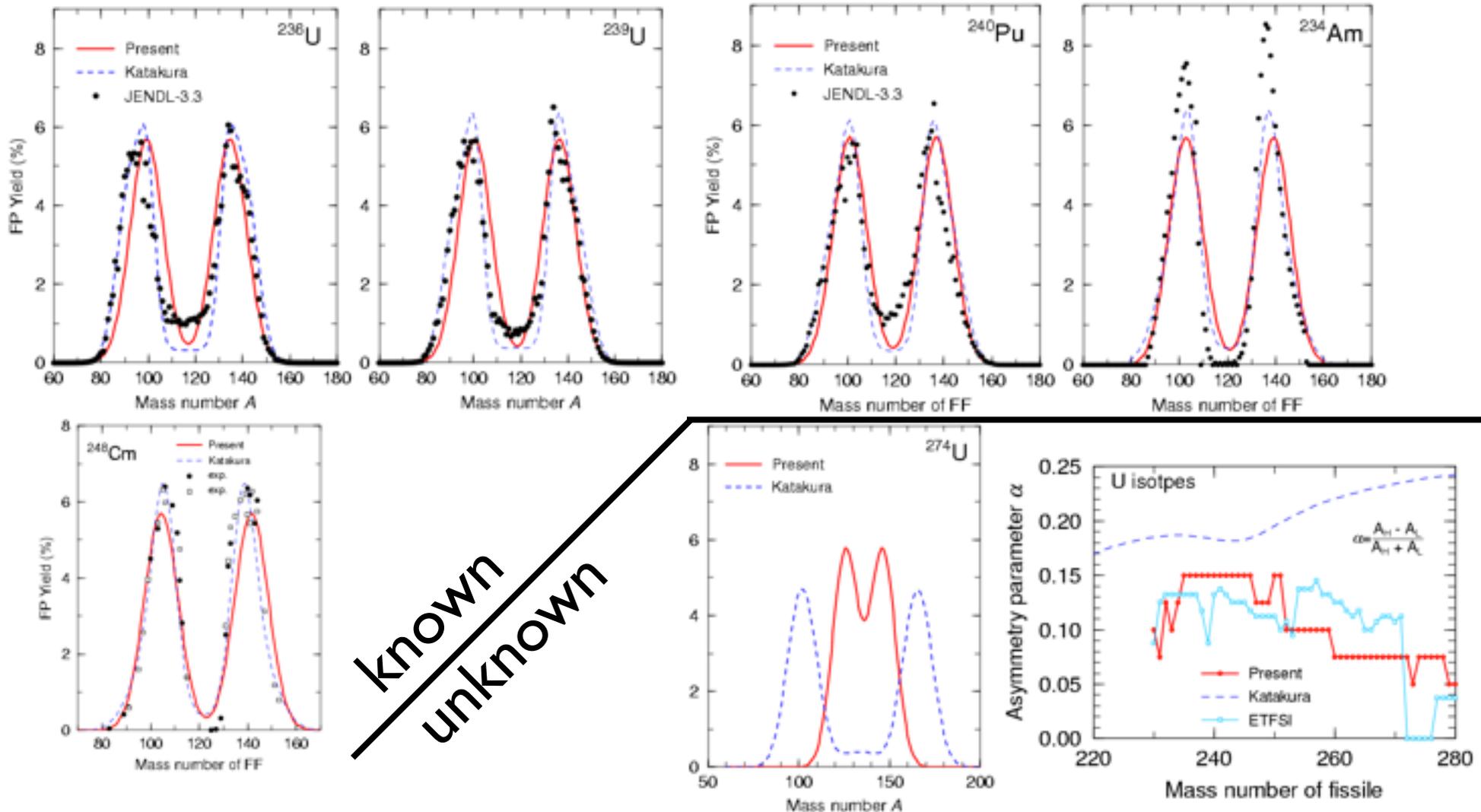


Symmetric-fissioning region:
 Located around
 ^{264}Fm ($Z=100, N=164$)

↑
Double of
 ^{132}Sn ($Z=50,$
 $N=82$)

Results - ^{236}U , ^{239}U , ^{240}Pu , ^{234}Am , ^{248}Cm , ^{236}U

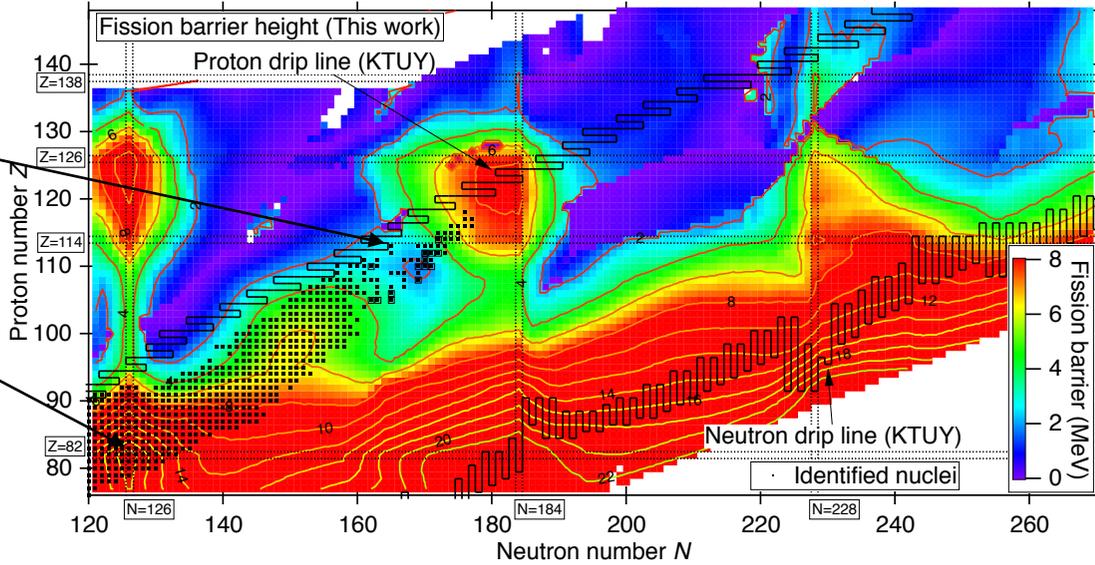
Distribution width: Sum of 3 gauss. on analysis of multi-dim. Langevin eq.



known
unknown

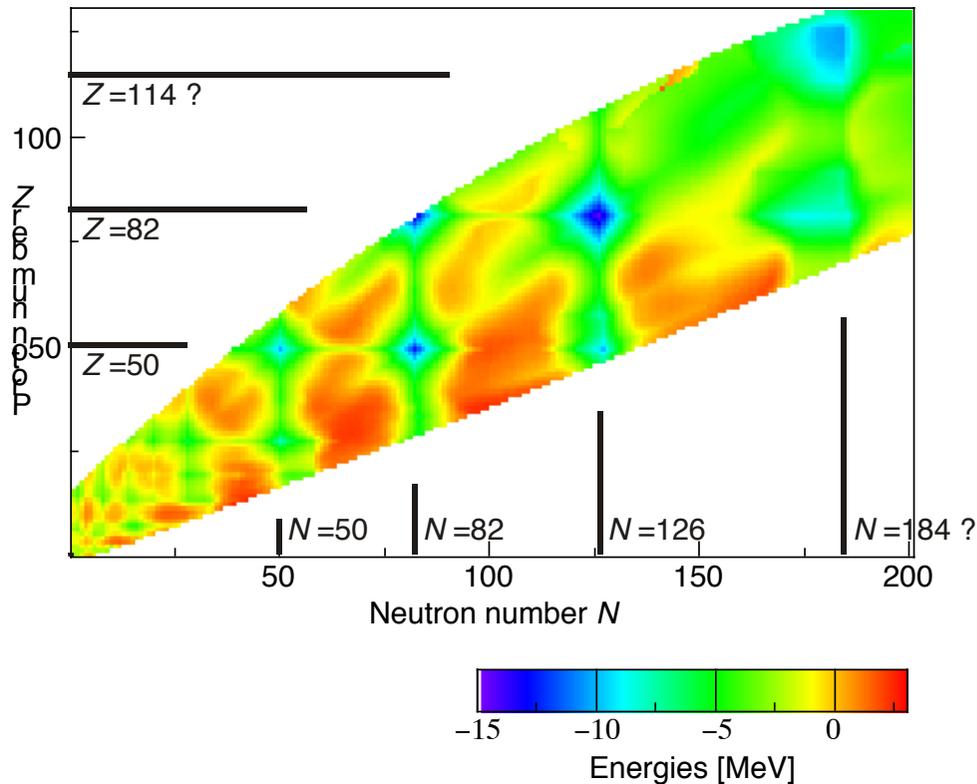
JENDL: Evaluated experimental data
Katakura: Empirical FFMD formula (function of A)

Nuclear mass and fission barrier height



Fission barrier height

Nuclear shell energies $E_{sh}(Z, N)$

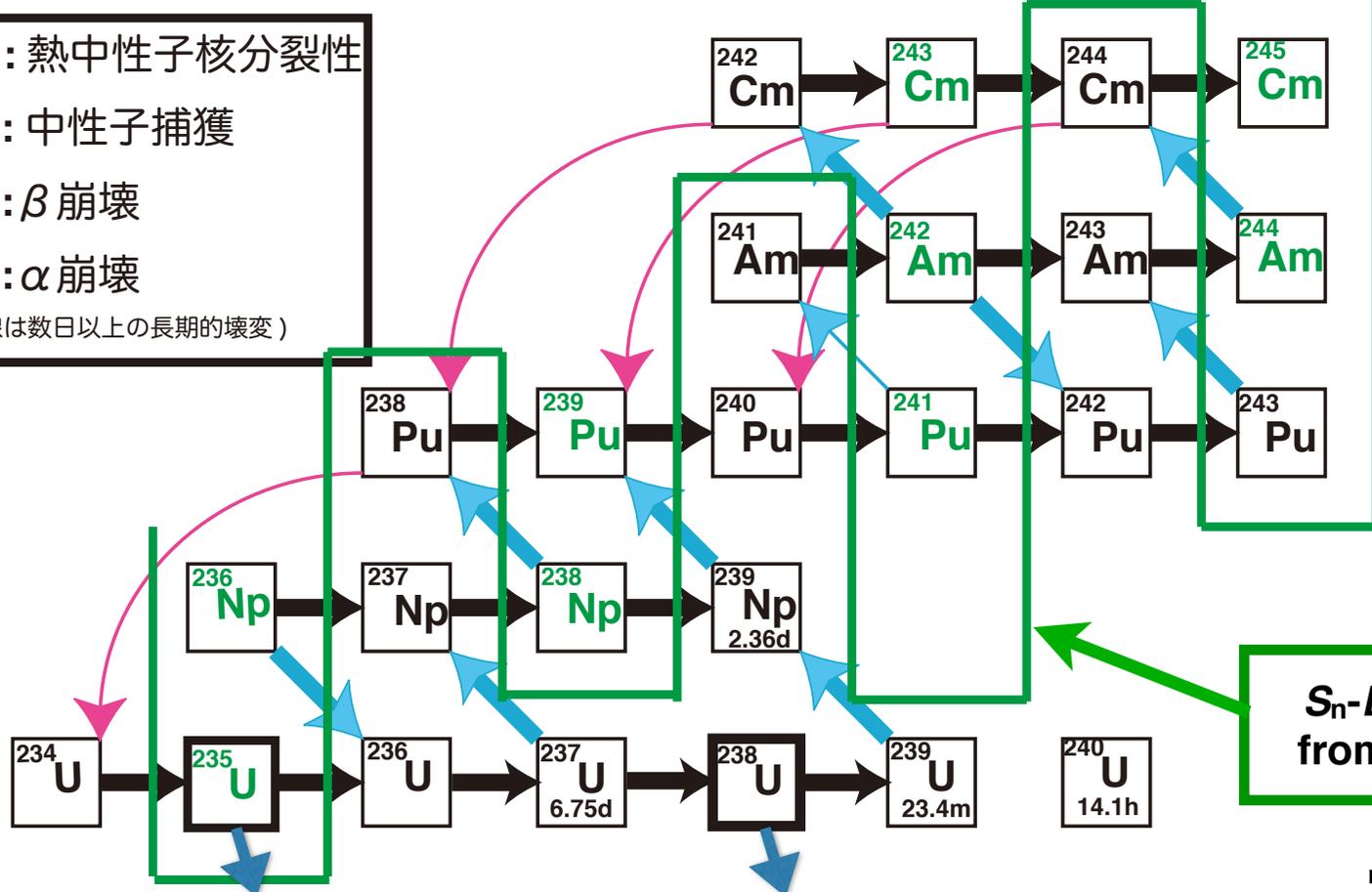


Nuclear shell energy

ウランと中性子の核反応

原子炉におけるアクチノイド核種の合成（燃焼）プロセス

Gr. : 熱中性子核分裂性
→ : 中性子捕獲
← : β 崩壊
↪ : α 崩壊
 (細線は数日以上の長期的壊変)



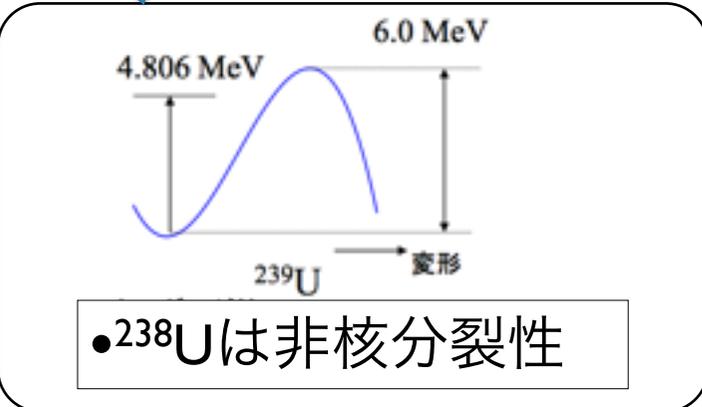
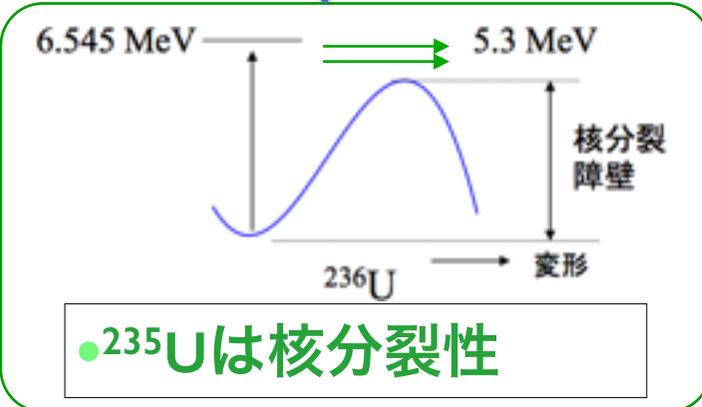
緑の線より上側が中性子誘起核分裂しやすい

**$S_n - B_{fiss} > 0$ (fissile)
from KTUY model**

ウランの同位体比(天然)

$$^{235}\text{U} : ^{238}\text{U} = 0.7 : 99.7$$

これを利用

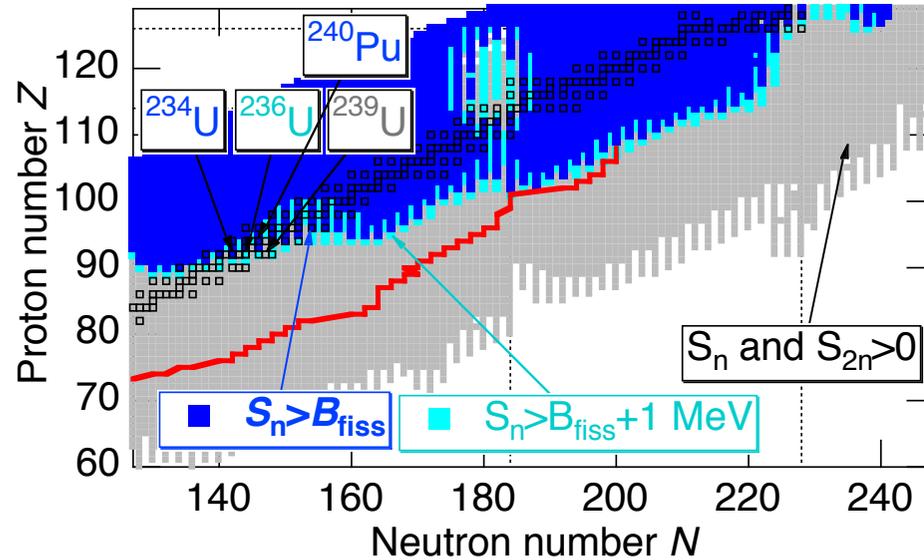
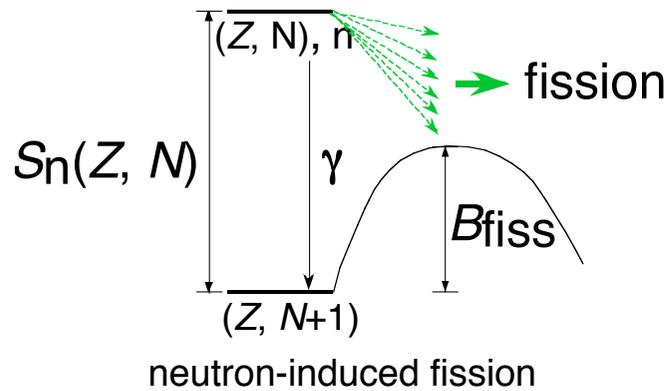


2. β -delayed fission (β -df) probability

Region of β -delayed and n-induced fission

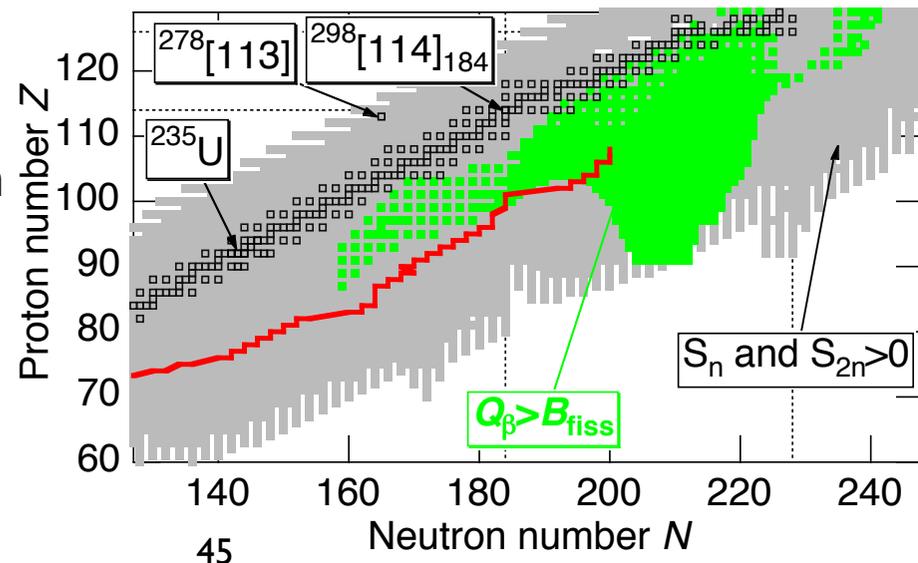
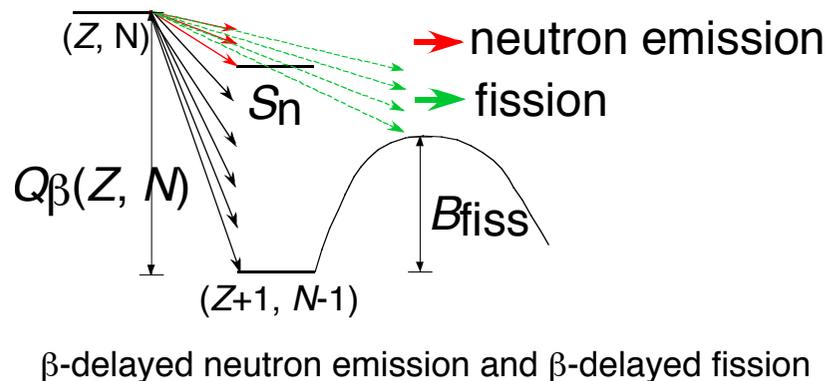
Nuclear masses and fission barrier:
KTUY (Koura-Tachibana-Uno-Yamada) mass formula

● n-induced fission



$$S_n > B_{fiss}$$

● β -delayed fission



$$Q_\beta > B_{fiss}$$

β -delayed fission probability P_f

β -delayed fission or neutron probability

$$P_k = \frac{C}{\lambda} \int_{-Q_\beta}^0 S_\beta(E) f(-E) \frac{\Gamma_k}{\Gamma_n + \Gamma_\gamma + \Gamma_f} dE$$

$k = f$: delayed fission

$k = n$: delayed neutron

Gross Theory of β -decay

(Tachibana, Yamada)

$S_\beta(E)$: β -strength function

λ : decay const. of β -decay

$f(-E)$: Fermi function

KTUY mass formula

Q_β : β -decay Q-value

S_n : neutron sep. energy

B_f : fission barrier height

δW : shell energy

Decay width Γ_n and Γ_f

$$\Gamma_n(E) = \frac{1}{2\pi} \frac{1}{\rho(E)} \frac{2MR^2}{\hbar^2} g \int_0^{E-S_n} \rho^*(E-S-\epsilon) \epsilon d\epsilon$$

$$\Gamma_f(E) = \frac{1}{2\pi} \frac{1}{\rho(E)} \int_{-\infty}^{E-B_f} \frac{\rho^*(E-S-\epsilon)}{1 + \exp(-2\pi E/\hbar\omega)} d\epsilon$$

Level density formula (Gilbert-Cameron type)

$$\rho_{GC}(E_x, J) = \frac{1}{12\sigma\sqrt{2}} \frac{\exp(2\sqrt{aU})}{a^{1/4}U^{5/4}} \frac{2J+1}{2\sigma^2} \exp\left(-\frac{(J+1/2)^2}{2\sigma^2}\right)$$

$$\rightarrow \rho_{GC}(E_x) = \frac{1}{12\sigma\sqrt{2}} \frac{\exp(2\sqrt{aU})}{a^{1/4}U^{5/4}} \text{ (MeV}^{-1}\text{)}$$

Phenom. formula

(Kawano, Chiba, HK, JNST 43 (2006))

$$E_x = U + A$$

$$\sigma = C^{1/2} A^{5/6} (U/A)^{1/4}$$

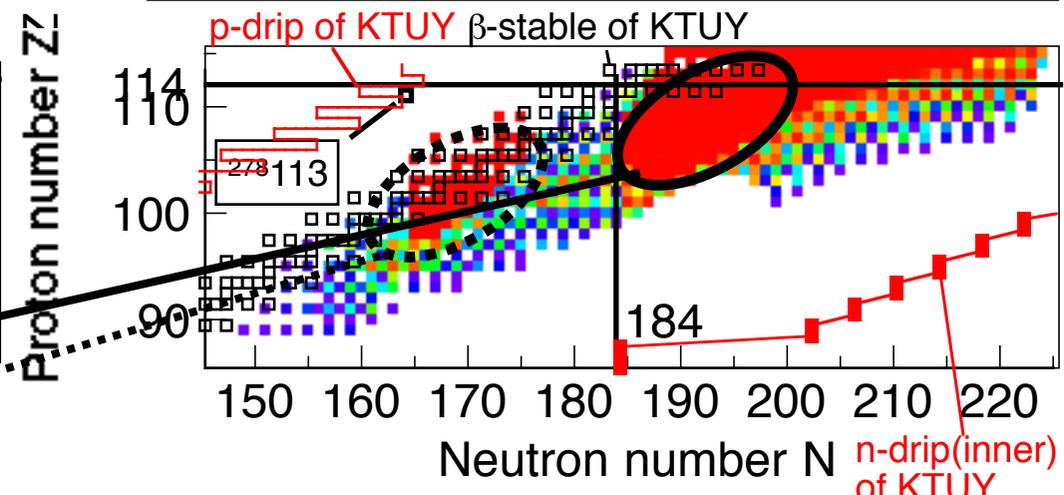
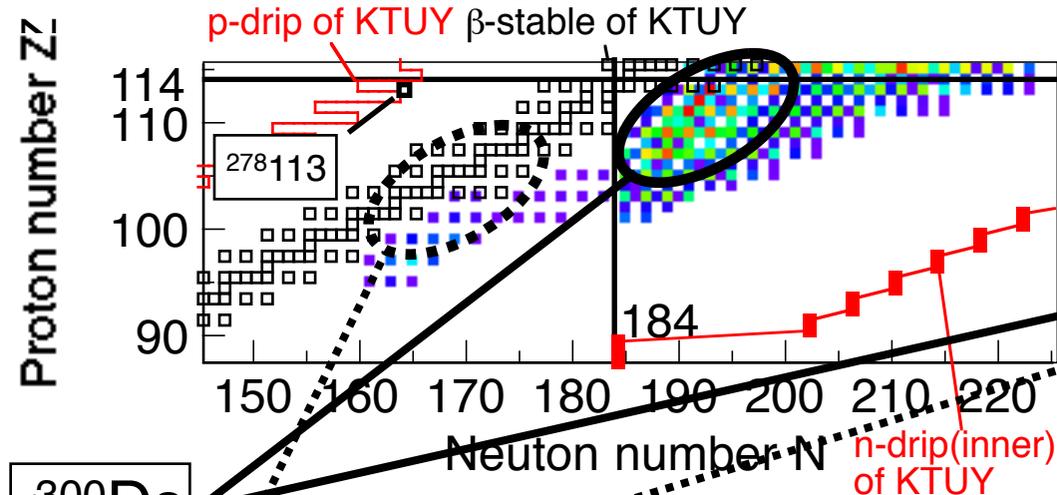
$$a = a^* \left\{ 1 + \frac{\delta W}{U} (1 - e^{-\gamma U}) \right\}$$

Tachibana

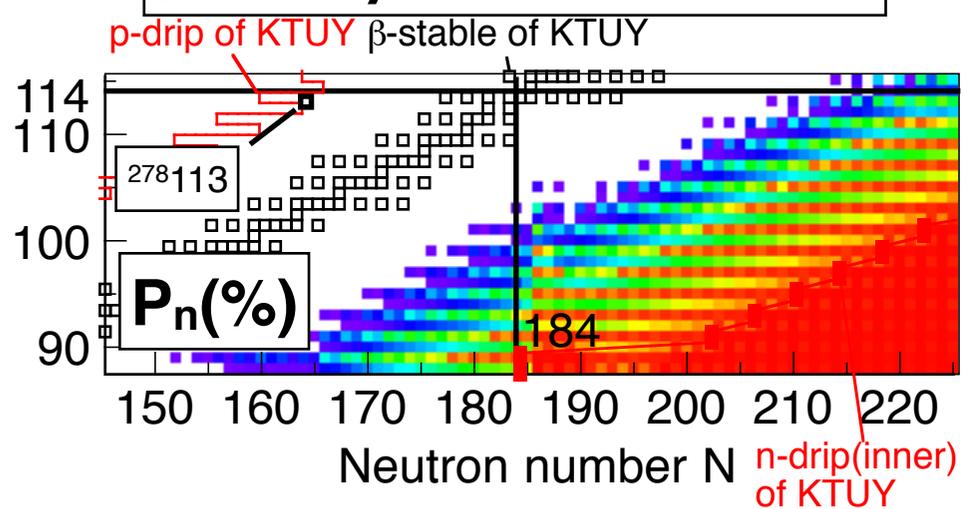
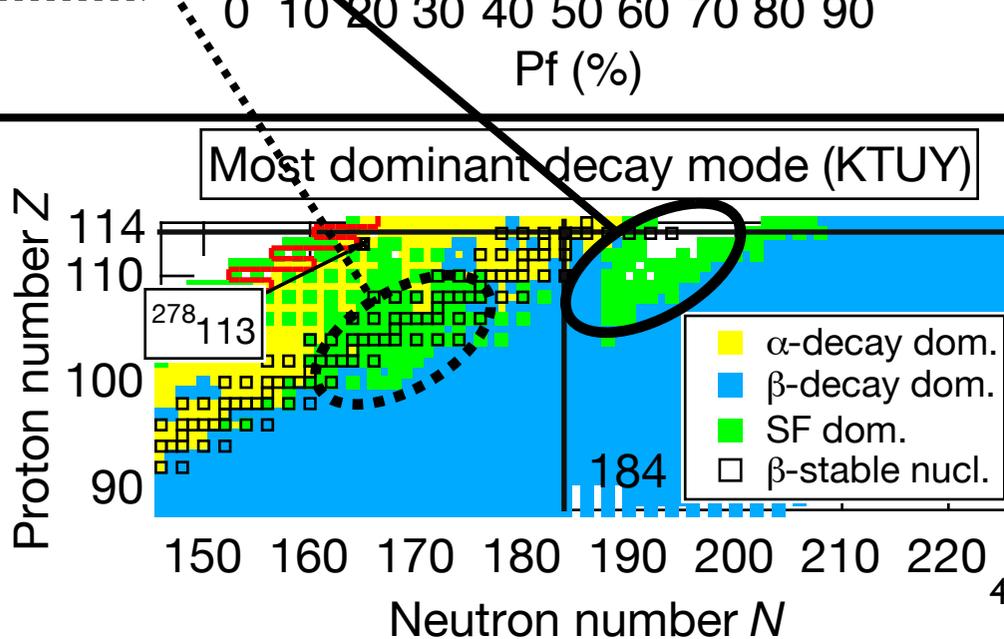
Results - β -delayed fission probability P_f

P_f (no correction)

P_f (B_f is 3MeV reduced)



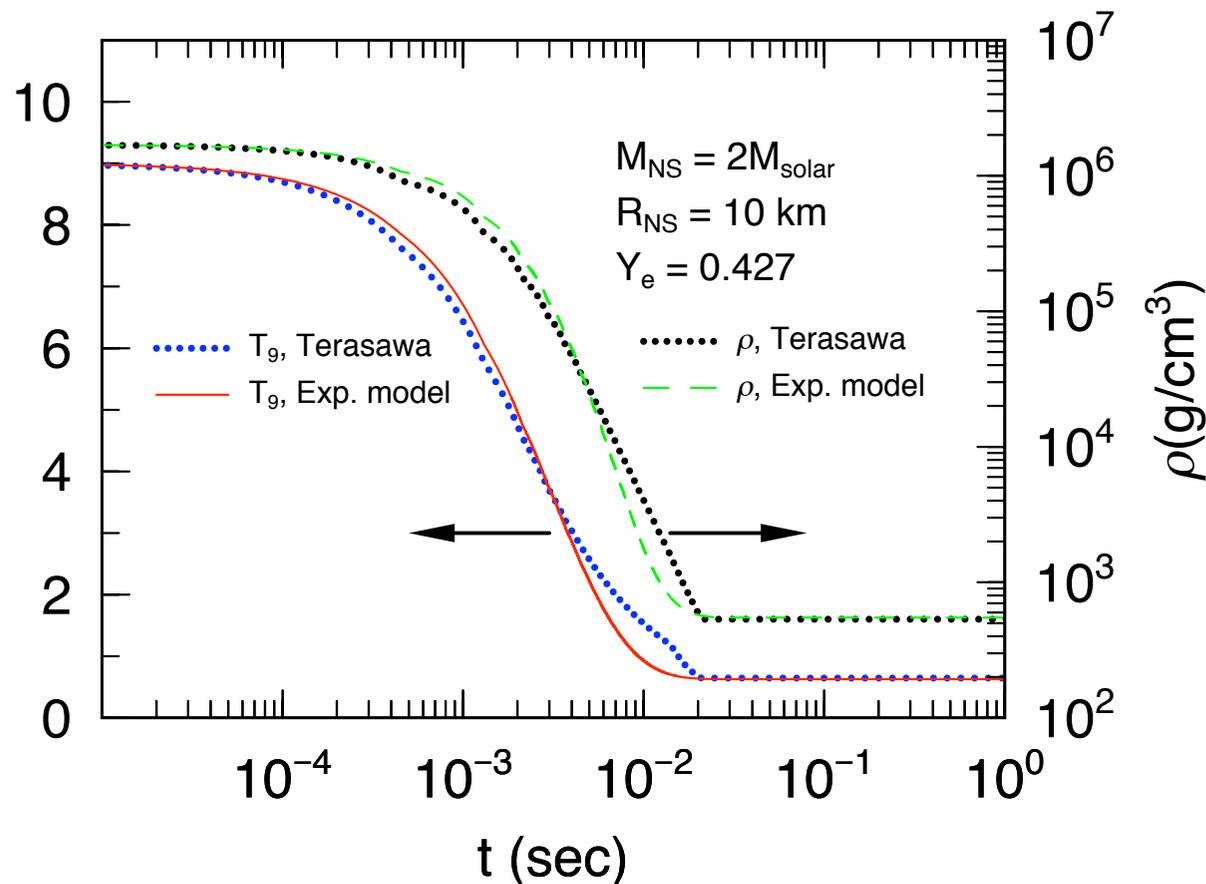
β -delayed neutron P_n



3. Effect of β -df to r-process abundance

R-process network calculation

Trajectory of supernova matter



exponential model

$$T_9 = T_{90} \exp(-t/T_{\text{ex}}) + 0.7$$

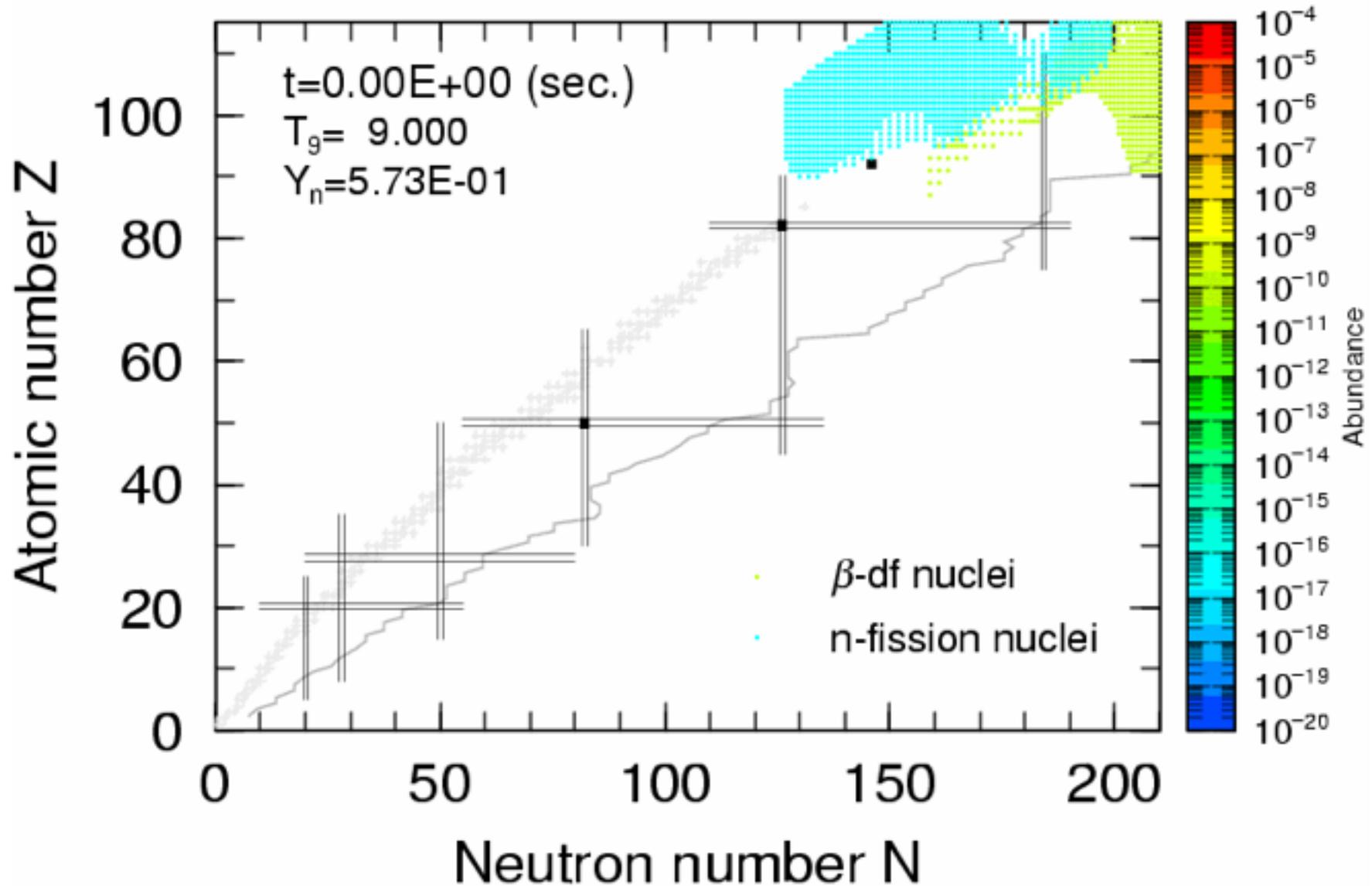
$$\rho(t) = \frac{3.33 \times 10^5 T_9(t)^3}{S}$$

$$T_9(t=0) = 9$$

Considered fission: only β -delayed fission

Time evolution of the r- process

$$S=200, B_f \rightarrow B_{fKTUY}-3\text{MeV}$$

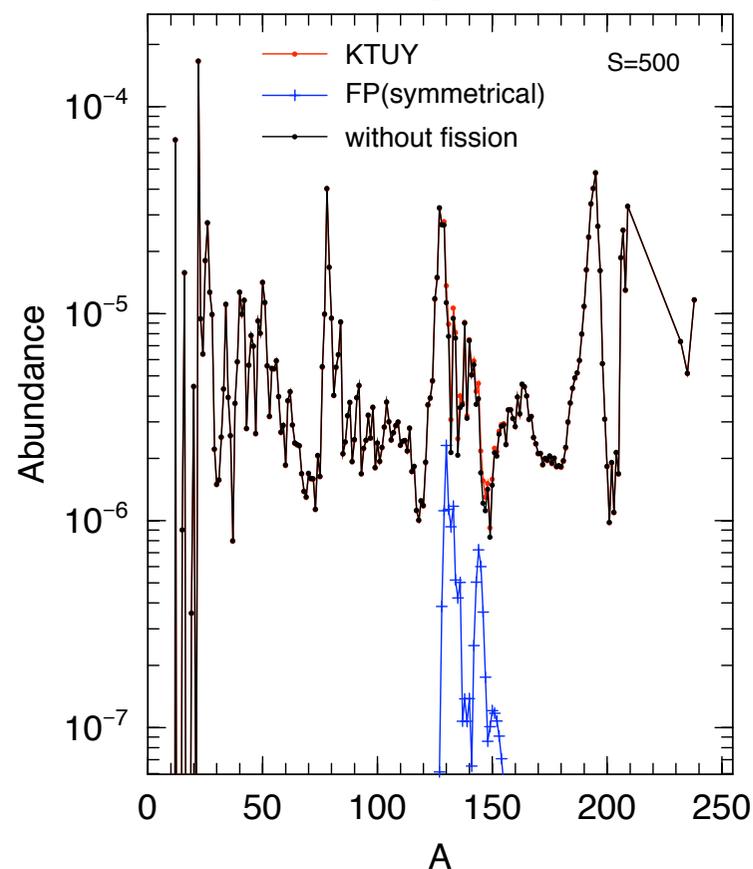
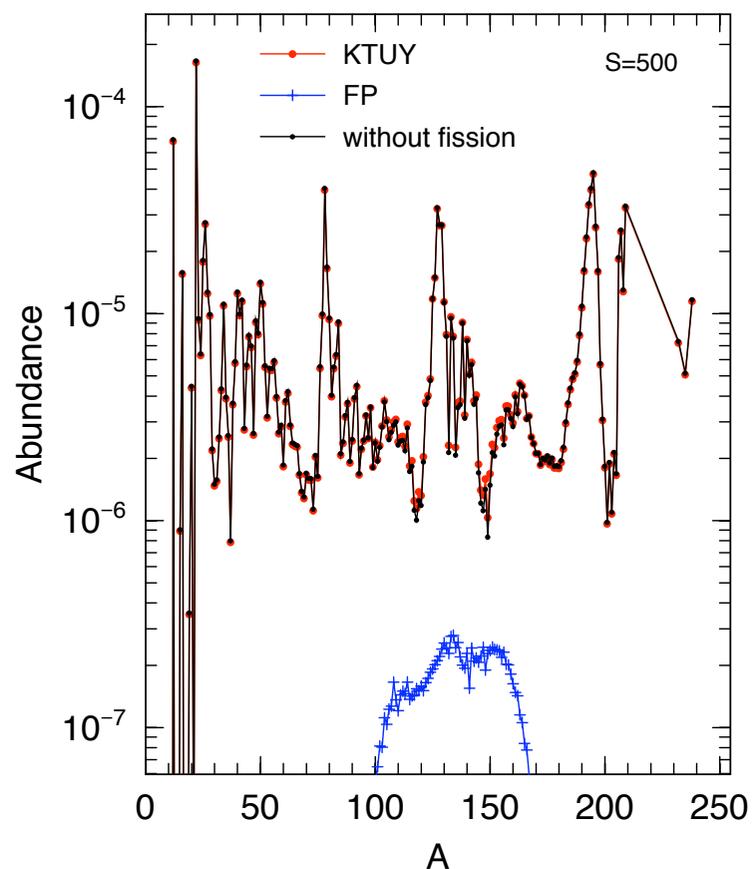


Results -r-process abundances (fission effect)

$$S=200, B_f \rightarrow B_{fKTUY}$$

FFMD: 2-center shell.

FFMD: Symmetric



Little contribution to r process

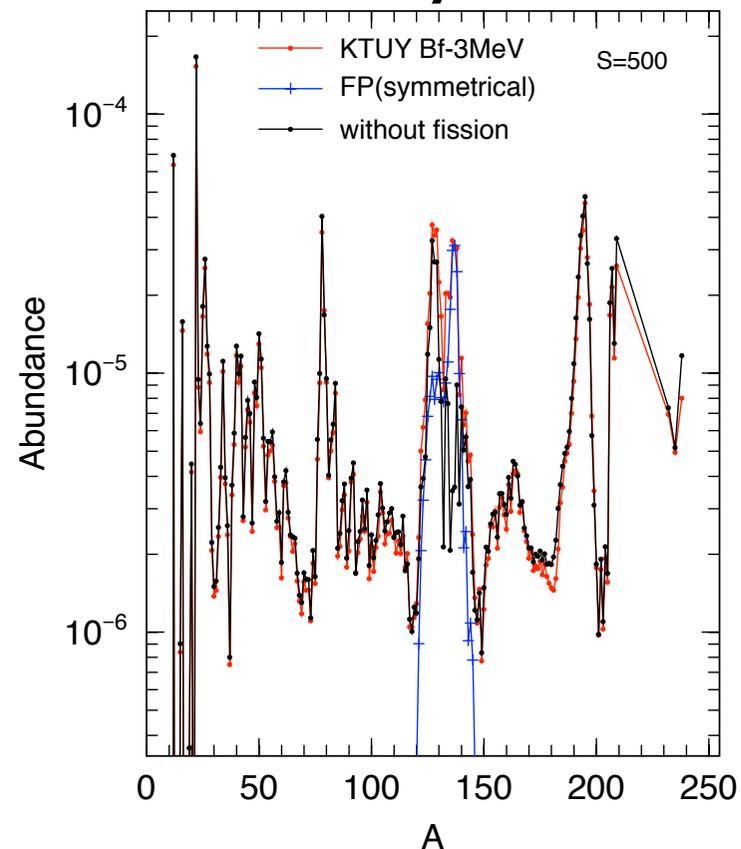
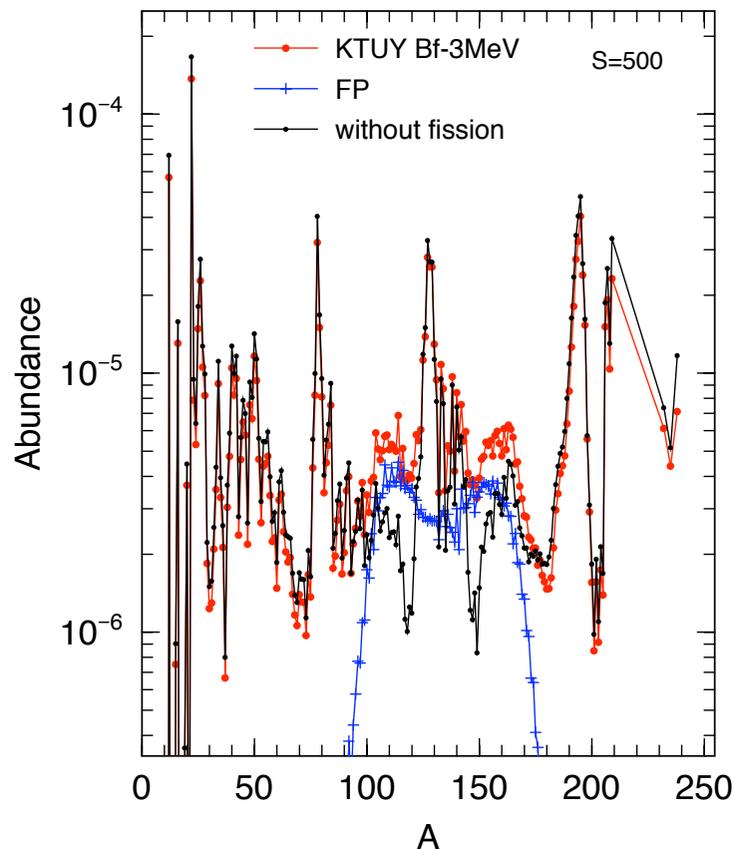
-> To check the effect of fission, we reduce fission barrier by 3MeV.

Results -r-process abundances (fission effect)

$$S=200, B_f \rightarrow B_{fKTUY}-3\text{MeV}$$

FFMD: 2-center shell.

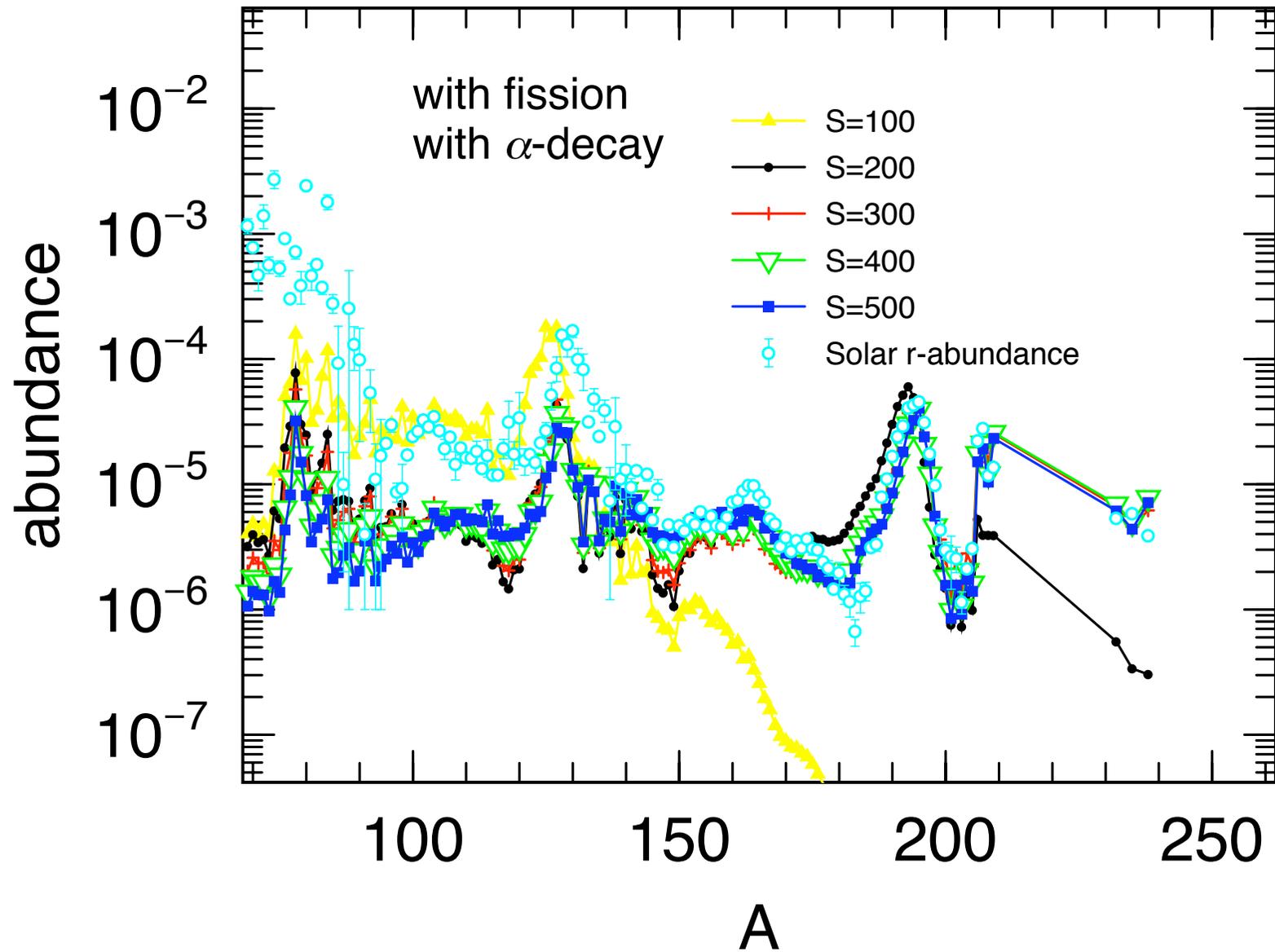
FFMD: Symmetric



Accumulated fission mass fragments could compensate $A \sim 110, 150$ region.

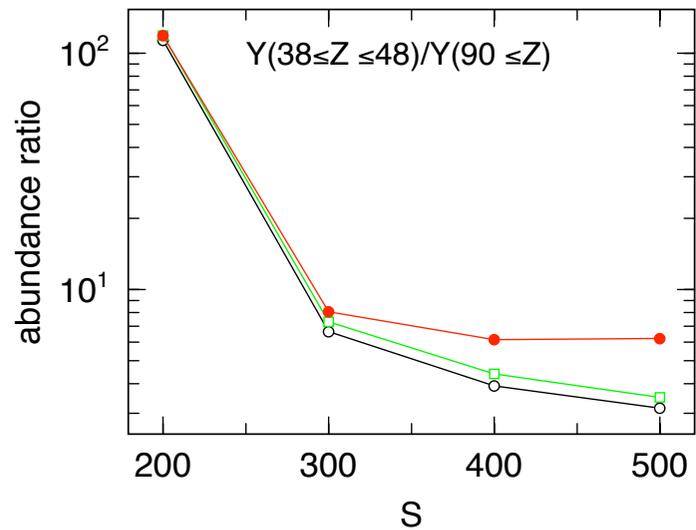
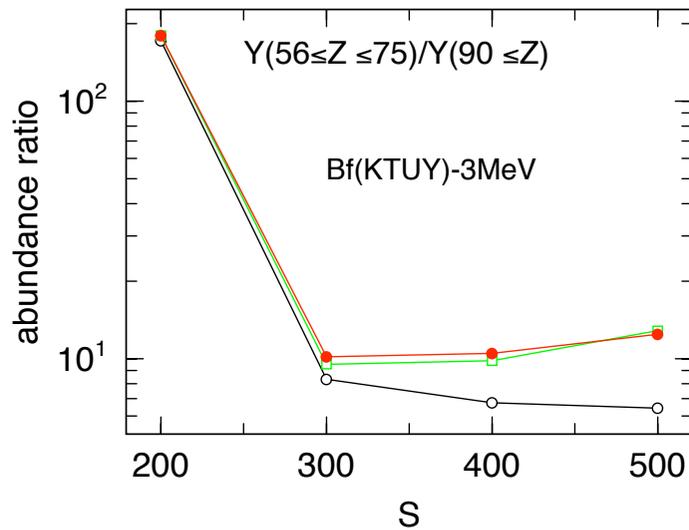
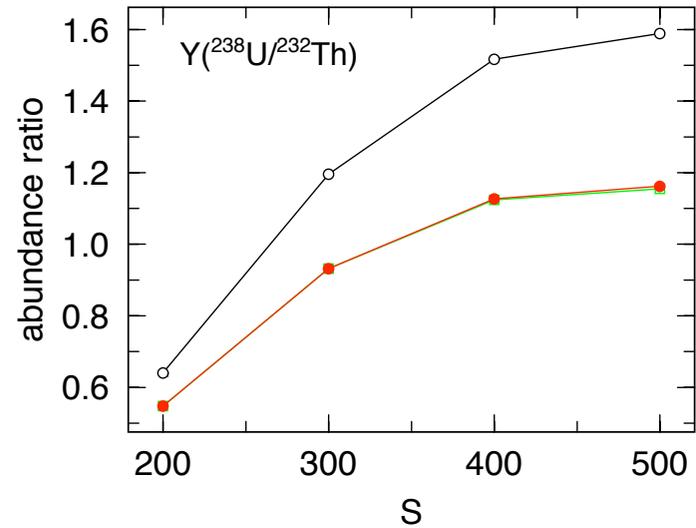
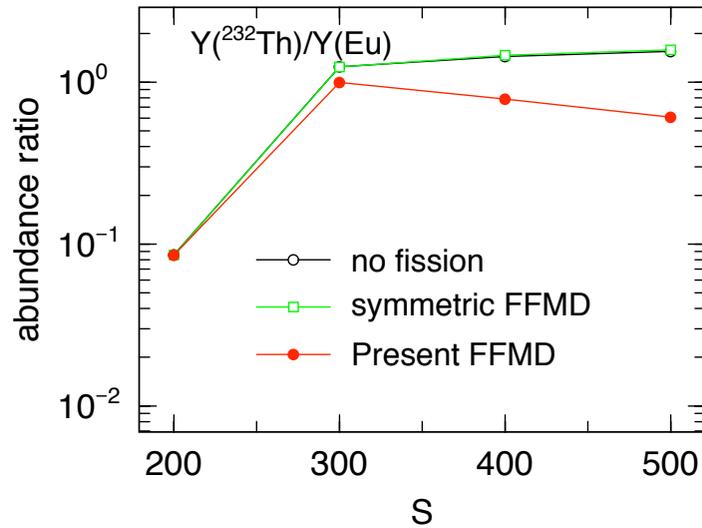
(depends on predicted fission barrier heights)

Results -r-process abundances (S-dependency)



Results - S-dependency of isotope ratio

$$B_f \rightarrow B_{fKTUY} - 3\text{MeV}$$



Summary

Bulk properties of nuclei

- **Current status of experimental nuclei**

- Recent data are reviewed by using the JAEA Chart of the Nuclides 2014

- **KTUY mass model (Spherical-basis method)**

- Calculation of masses and fission barrier is reviewed

R-process and fission

From Nuclear Physics of superheavy nuclei:

- **Fission mass fragment calculation from a two-center shell model**

- Symmetric fission region is rather localized around $^{264}\text{Fm}(100,164)$.

- **Beta-delayed fission probability from the KTUY mass model**

- Region with large P_f is rather localized around $^{300}\text{Ds}(110,190)$.

From the r-process study:

- **Reaction Network calculation**

- Fission fragment tends to compensate a discrepancy near $A=110$ and 140 region (without adopting an $N=82$ quenching) *Qualitatively!*

- S has to be larger than 2-300 or more? (by considering in our model. More analysis is required.)